THE EGNOG SURVEY: GAS EXCITATION IN NORMAL GALAXIES AT $Z \approx 0.3$

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ABSTRACT

As observations of molecular gas in galaxies are pushed to lower star formation rate galaxies at higher redshifts, it is becoming increasingly important to understand the conditions of the gas in these systems to properly infer their molecular gas content. The rotational transitions of the carbon monoxide (CO) molecule provide an excellent probe of the gas excitation conditions in these galaxies. In this paper we present the results from the gas excitation sample of the Evolution of molecular Gas in Normal Galaxies (EGNoG) survey at the Combined Array for Research in Millimeter-wave Astronomy (CARMA). This subset of the full EGNoG sample consists of four galaxies at $z \approx 0.3$ with star formation rates of $40 - 65 \text{ M}_{\odot} \text{ yr}^{-1}$ and stellar masses of $\approx 2 \times 10^{11} \text{ M}_{\odot}$. Using the 3 mm and 1 mm bands at CARMA, we observe both the $\text{CO}(J = 1 \rightarrow 0)$ and $\text{CO}(J = 3 \rightarrow 2)$ transitions in these four galaxies in order to probe the excitation of the molecular gas. We report robust detections of both lines in three galaxies (and an upper limit on the fourth), with an average line ratio, $r_{31} = L'_{\rm CO(3-2)}/L'_{\rm CO(1-0)}$, of 0.46 ± 0.07 (with systematic errors $\leq 40\%$), which implies sub-thermal excitation of the CO($J = 3 \rightarrow 2$) line. We conclude that the excitation of the gas in these massive, highly star-forming galaxies is consistent with normal star-forming galaxies such as local spirals, not starbursting systems like local ultra-luminous infrared galaxies. Since the EGNoG gas excitation sample galaxies are selected from the main sequence of star-forming galaxies, we suggest that this result is applicable to studies of main sequence galaxies at intermediate and high redshifts, supporting the assumptions made in studies that find molecular gas fractions in star forming galaxies at $z \sim 1-2$ to be an order of magnitude larger than what is observed locally.

Subject headings: Galaxies:evolution — Galaxies: high-redshift — Galaxies:ISM

1. INTRODUCTION

In the past decade, molecular gas observations have begun probing the high redshift universe in a systematic way using increasingly powerful millimeter instruments. The picture that is emerging at redshifts 1-2 is similar in some respects to what we see in the local universe. Sub-mm galaxies (SMGs) are observed to be undergoing extreme starbursts as a result of major interactions or mergers (e.g. Sheth et al. 2004; Tacconi et al. 2008; Engel et al. 2010), equivalent to local ultra-luminous infrared galaxies (ULIRGs) (e.g. Sanders et al. 1986; Solomon et al. 1997; Downes & Solomon 1998). Starforming galaxies at high redshifts akin to local spirals are becoming accessible as well. Recent works (Tacconi et al. 2010; Daddi et al. 2010; see also work by Baker et al. 2004 on a z = 2.7 Lyman break galaxy) suggest that $z \sim 1-2$ star-forming galaxies (with star formation rates (SFRs) of $\approx 50 - 200 \text{ M}_{\odot} \text{ yr}^{-1}$) are scaled up versions of local spirals, forming stars in a steady mode (not triggered by interaction), despite hosting star formation rates at the level of typical local starburst systems like luminous infrared galaxies (LIRGs) and ULIRGS.

While galaxies classified as LIRGs or ULIRGs (by their infrared luminosities only) have typically been associated with starbursting and merging systems by analogy to

galaxies in the local universe, it is becoming clear that this connection does not hold at high redshifts. Morphological studies find that while 50% of local LIRGs show evidence for major mergers (Wang et al. 2006), that fraction appears to decrease toward high redshifts: Bell et al. (2005) find that more than half of intensely star-forming galaxies at $z \approx 0.7$ have spiral morphologies and fewer than 30% show evidence of strong interaction. Further, the typical SFR of (normal) star-forming galaxies (like local spirals) increases toward higher redshift. Starforming galaxies have been observed to obey a tight relation between stellar mass and star formation rate out to $z \sim 2.5$ (e.g. Brinchmann et al. 2004; Noeske et al. 2007; Elbaz et al. 2007; Daddi et al. 2007; Pannella et al. 2009; Elbaz et al. 2011; Karim et al. 2011). This 'main sequence' defines what is normal for star-forming galaxies as a function of redshift, showing that typical SFRs increase with redshift. Throughout this work, we use SFG to refer to main sequence (normal) star-forming galaxies.

The increase in the star formation rate is mirrored in the molecular gas fraction of these systems. While studies of local spirals (e.g. FCRAO survey, Young et al. 1995; BIMA SONG, Regan et al. 2001, Helfer et al. 2003; HERACLES, Leroy et al. 2009; also Combes et al. 1994; Kuno et al. 2007) find average molecular gas fractions $f_{\rm mgas} = M_{\rm mgas}/(M_* + M_{\rm mgas}) \sim 5\%$ (where $M_{\rm mgas}$ is the molecular gas mass (including He) and M_* is the stellar mass), observations of high redshift SFGs suggest molecular gas fractions of 20-80%, an order of magnitude higher than local spirals. It is clear that in order to understand these SFGs at $z \sim 1-2$, we must investigate the condition of the molecular gas which is forming stars at such an enhanced rate. Do these systems truly hold massive reservoirs of molecular gas or is enhanced excitation of the gas misleading the interpretation of the observations?

The rotational transitions of the carbon monoxide (CO) molecule provide a direct probe of the excitation of the molecular gas in galaxies. Local starburst galaxies and ULIRGs (e.g. Bayet et al. 2004; Weiß et al. 2005b; Papadopoulos et al. 2007; Greve et al. 2009) and high redshift SMGs and quasars (e.g. Weiß et al. 2005a; Riechers et al. 2006; Weiß et al. 2007; Riechers 2011; Riechers et al. 2011) show signatures of excited molecular gas: observed CO line spectral energy distributions peak at $J_{upper} > 5$ with thermalized lines up to $J_{upper} >$ 3. In contrast, studies of the Milky Way (Fixsen et al. 1999) and local SFGs (e.g. Mauersberger et al. 1999; Yao et al. 2003; Mao et al. 2010) find a wide spread of excitation conditions, with an average that implies lessexcited gas, where the $J_{upper} = 3$ line is already subthermal. This suggests that the $CO(J = 3 \rightarrow 2)$ line in particular is an indicator of the star formation character of a galaxy: 'starburst' versus 'normal'.

More important still, the ratio of higher rotational lines of CO to the $CO(J = 1 \rightarrow 0)$ line is *necessary* to translate the observed CO line luminosity to a molecular gas mass using X_{CO} or α_{CO} , since this conversion factor is calibrated for the $CO(J = 1 \rightarrow 0)$ luminosity. Therefore, the measurement of $r_{J1} = L'_{CO(J-(J-1))}/L'_{CO(1-0)}$ not only informs our interpretation of the current intermediate and high redshift CO line studies, but is critical in the era of ALMA, which provides an order of magnitude increase in sensitivity, making the CO lines in high redshift galaxies more accessible. The $CO(J = 3 \rightarrow 2)$ line in particular, observed in the 1mm, 2mm and 3mm bands, probes the molecular gas in galaxies at $z \sim 0.3-3$. This redshift range is of particular interest since it includes the peak of the star formation rate density of the universe $(z \sim 1 - 2)$ and therefore the height of galaxy building.

While several studies have measured r_{31} in the local universe (Mauersberger et al. 1999; Yao et al. 2003; Mao et al. 2010; Papadopoulos et al. 2011), the measurement of line ratios in intermediate and high redshift galaxies has mostly been limited to SMGs and quasars (see the review by Solomon & Vanden Bout 2005). Our knowledge of CO line ratios in SFGs at $z \sim 1-2$ is limited to one study at z = 1.5 (presented in two papers: Dannerbauer et al. 2009 and Aravena et al. 2010) which measures r_{21} in three galaxies and r_{31} in one galaxy. It is clear that more work is needed to better constrain the line ratios in intermediate and high redshift SFGs to interpret existing and future data and better understand the state of the molecular gas in these systems.

As part of the Evolution of molecular Gas in Normal Galaxies (EGNoG) survey, we observe both the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ lines in four galaxies at $z \approx 0.3$ (the gas excitation sample), more than doubling the number of SFGs at z > 0.1 in which CO line ratios

have been measured. In this paper, we present the r_{31} values for the EGNoG gas excitation sample and compare to previous work at low and high redshifts. We discuss the implications of this measurement for the excitation of the molecular gas in the observed galaxies as well as for high-redshift SFGs.

The paper is organized as follows: in Section 2 we give a brief description of the EGNoG survey as a whole, describe the selection of the gas excitation sample and present the redshifts, SFRs and stellar masses of the galaxies in this work; in Section 3 we describe the observations and data reduction; in Section 4 we present the analysis of r_{31} in these galaxies; in Section 5 we discuss the implications of this work; and we give some concluding remarks in Section 6. The data reduction and measurement of fluxes is discussed in detail in Appendix A and moment maps of the detected CO emission are presented in Appendix B. Throughout this work, we use a Λ CDM cosmology with (h, Ω_M , Ω_Λ) = (0.7, 0.3, 0.7).

2. THE EGNOG SURVEY

The EGNoG survey is a key project at the Combined Array for Research in Millimeter-wave Astronomy (CARMA).¹ By observing rotational lines of the ¹²CO molecule, the EGNoG survey traces the molecular gas in 31 galaxies from z = 0.05 to 0.5, where the significant evolution from gas-rich galaxies at $z \sim 1-2$ (Daddi et al. 2010; Tacconi et al. 2010) to relatively gaspoor local galaxies (e.g. BIMA SONG, Helfer et al. 2003; HERACLES, Leroy et al. 2009; CARMA STING, Rahman et al. 2012) remains almost entirely unobserved. The full EGNoG sample is split into 4 redshift bins: bin A, 13 sources, z = 0.05 - 0.1; bin B, 10 sources, z = 0.16 - 0.20; bin C, 4 sources, z = 0.28 - 0.32; and bin D, 4 sources, z = 0.47 - 0.53. The full survey is presented in the forthcoming paper Bauermeister et al. 2012b (in preparation).

In this paper (Bauermeister et al. 2012a), we present the gas excitation sample (bin C) of the EGNoG survey, the subset of the full survey sample for which we observe both the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ lines. Observations were made using the CARMA 15-element array with the 3mm band (single-polarization) for the $CO(J = 1 \rightarrow 0)$ observations and the 1mm band (dualpolarization) for the $CO(J = 3 \rightarrow 2)$ observations.

2.1. Sample Selection

The galaxies of EGNoG bin C are drawn from the main spectroscopic sample of the Sloan Digital Sky Survey (SDSS), Data Release 7 (York et al. 2000; Strauss et al. 2002; Abazajian et al. 2009). The galaxies were selected from the parent sample to be as representative as possible of the main sequence of star-forming galaxies. The main sequence is the tight correlation between M_* and SFR that has been observed over a large range of redshifts: e.g. $z \sim 0$ (Brinchmann et al. 2004), $z \sim 0.2 - 1$ (Noeske et al. 2007), $z \sim 1 - 2$ (Elbaz et al. 2007; Daddi et al. 2007; Pannella et al. 2009), (see also the summary of recent results in Dutton et al. (2010)).

¹ CARMA is a 3-band, 23-element millimeter interferometer jointly operated by the California Institute of Technology, University of California Berkeley, University of Chicago, University of Illinois at Urbana-Champaign, and University of Maryland.

EGNoG: Gas Excitation

EGNoG	SDSS identification	RA	Dec	z	$\log(M_*/M_{\odot})$	SFR
Name						$({\rm M}_{\odot}~{\rm yr}^{-1})$
$C1^a$	SDSS J092831.94+252313.9	09:28:31.941	+25:23:13.925	0.283020 ± 0.000022	$11.24_{-0.11}^{+0.10}$	$38.7^{+85.9}_{-25.6}$
C2	SDSS J090636.69+162807.1	09:06:36.694	+16:28:07.136	0.300622 ± 0.000010	$11.20^{+0.29}_{-0.14}$	$57.5^{+90.1}_{-21.9}$
C3	SDSS J132047.13+160643.7	13:20:47.139	+16:06:43.720	0.312361 ± 0.000014	$11.46^{+0.25}_{-0.12}$	$64.9^{+142.9}_{-28.0}$
C4	SDSS J133849.18+403331.7	13:38:49.189	+40:33:31.748	0.285380 ± 0.000015	$11.26_{-0.12}^{+0.18}$	$50.5^{+48.1}_{-15.4}$

Table 1

Basic information. Derived quantities (z, M_*, SFR) are from the MPA-JHU group (see text). ^{*a*} indicates duplicate source in SDSS: the average value is reported for z, M_* and SFR.

Building on these observations, a few authors have attempted to describe the main sequence relation at $0 \le z \lesssim 2.5$ with one equation (Bouché et al. 2010; Karim et al. 2011; Elbaz et al. 2011). In order to classify the EGNoG galaxies, we adopt a relation which roughly agrees with the relations from Bouché et al. (2010), Karim et al. (2011) and Elbaz et al. (2011) (see Bauermeister et al. 2012b for a complete description):

$$sSFR_{\rm MS}({\rm Gyr}^{-1}) = 0.07(1+z)^{3.2} \left(\frac{M_*}{10^{11} {\rm M}_{\odot}}\right)^{-0.2}$$
(1)

where $sSFR_{MS}$ is the specific star formation rate (sSFR= SFR/M_*) of the main sequence (MS) of star-forming galaxies. We differentiate 'starburst' (SB) from 'normal' galaxies according the criteria of Rodighiero et al. (2011): $sSFR_{SB} > 4 \times sSFR_{MS}$. Therefore, SFGs (normal star-forming galaxies) lie roughly within a factor of 4 of the main sequence sSFR (which is a function of M_* and z) and starbursts lie at sSFR values larger than 4 times the main sequence sSFR.

In the selection of the EGNoG sample, we apply the following criteria in each redshift bin in order to identify non-interacting, star-forming galaxies lying as close to the main sequence as possible. Star-forming galaxies are selected using the BPT diagram (Baldwin et al. 1981) criteria from Kauffmann et al. (2003) (rejecting sources with active galactic nuclei). Obviously interacting galaxies were excluded via visual inspection of the SDSS optical images. However, some interacting galaxies may be in the sample due to the difficulty of identification at the modest resolution of the SDSS images. Practical considerations imposed the following further constraints. We required a spectroscopic redshift so that the error in the redshift is small enough to ensure that CO emission would be captured within the observed bandwidth. We excluded galaxies with SFRs below a minimum value estimated from the instrument sensitivity.

The result of the sample selection is illustrated in Figure 1, which shows stellar mass versus SFR of the EG-NoG bin C galaxies (red points). The blue shading indicates the (logarithm of the) density of points in the M_* - SFR plane for all star-forming galaxies (spectroscopic targets only; ≈ 1300 galaxies) at z = 0.25 - 0.35. We plot galaxies in a slightly larger redshift range than the bin C specification in order to better capture the behavior of the main sequence. The main sequence of star-forming galaxies at z = 0.3 is indicated by the solid black line, with the starburst cutoff indicated by the dashed black line. In this plot, the low-mass, low-SFR end of the main sequence is sparsely sampled due to the limited number of spectroscopically targeted, low-SFR, star-forming galaxies in the SDSS at $z \approx 0.3$. While the EGNoG bin C galaxies are high- M_* , high-SFR galaxes, they lie within the expected scatter of the main sequence (as defined in Equation 1), and are not classified as starburst galaxies according to the prescription from Rodighiero et al. (2011) (presented above).

2.2. Redshifts, Stellar Masses and Star Formation Rates

Spectroscopic redshifts are from David Schlegel's spZbest files produced by the Princeton-1D code, specBS². The stellar masses and SFRs of galaxies in the SDSS DR7 are provided by the Max-Planck-Institute for Astrophysics - John Hopkins University group (http://www.mpa-garching.mpg.de/SDSS). Stellar masses are derived by fitting SDSS ugriz photometry to a grid of models spanning a wide range of star formation histories. This method is found to compare quite well with the Kauffmann et al. (2003) methodology using spectral features (more detail on this comparison is found on the website above). Star formation rates are derived by fitting the fluxes of no less than 5 emission lines using the method described in Brinchmann et al. (2004). Both stellar masses and star formation rates are derived using a Bayesian analysis, producing probability distributions of each quantity for each galaxy. These distributions for the four bin C galaxies are shown in Figure 2. We take



Figure 1. Stellar mass versus SFR in EGNoG bin C. Red points and error bars show EGNoG galaxies and blue shading shows the logarithm of the density (in the M_* -SFR plane) of star-forming galaxies from the parent dataset at z = 0.25 - 0.35 (slightly larger than the EGNoG redshift range so that more points may be included to better capture the behavior of the main sequence). The solid black line indicates the main sequence (Equation 1) at the average redshift of the bin. The starburst (SB) criterion is indicated by the black dashed line.

² See http://spectro.princeton.edu/ for more information



Figure 2. Probability distribution functions for the stellar masses (left panel) and star formation rates (right panel) from the MPA-JHU group for bin C sources. Data points give the 2.5, 16, 50, 84 and 97.5 percentiles of the distributions. The median, mean and mode are indicated by the vertical solid, dashed and dotted lines respectively. In cases where a duplicate exists (source C1), the duplicate values are plotted in red.

the median of the distribution, with errors indicated by the 16th and 84th percentile points. In the case where a duplicate SDSS source exists (as a result of SDSS automated source-finding), we take the average of the two median values and use the lowest(highest) 16th(84th) percentile value to indicate the negative(positive) error. The redshifts, stellar masses and star formation rates (with errors) are given in Table 1.

3. CARMA OBSERVATIONS

The four bin C galaxies were observed in two rotational transitions of the CO molecule: $\text{CO}(J = 1 \rightarrow 0)$ $\nu_{\text{rest}} = 115.3 \text{ GHz}, \nu_{\text{obs}} \sim 88 \text{ GHz}$ and $\text{CO}(J = 3 \rightarrow 2)$ $\nu_{\text{rest}} = 345.9 \text{ GHz}, \nu_{\text{obs}} \sim 266 \text{ GHz}$. At each frequency, each galaxy was observed over several different days. Each dataset includes observations of a nearby quasar for phase calibration (taken every 15-20 minutes), a bright quasar for passband calibration and either Mars or MWC349 for flux calibration (in most cases).

The reduction of all observations for this survey was carried out within the EGN³ data reduction infrastructure (based on the MIS pipeline; Pound & Teuben 2012) using the Multichannel Image Reconstruction, Image Analysis and Display (MIRIAD; Sault et al. 2011) package for radio interferometer data reduction. Our data analysis also used the miriad-python software package (Williams et al. 2012). The data were flagged, passband-calibrated and phase calibrated in the standard way. Final images were created using invert with options=mosaic in order to properly handle and correct for the three different primary beam patterns. All observations are single-pointing. We describe the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ observations individually below. A full description of the data reduction and flux measurement is given in Appendix A.

3.1. $CO(J = 1 \to 0)$

The $CO(J = 1 \rightarrow 0)$ transition for the galaxies presented here lies in the 3 mm band of CARMA (singlepolarization, linearly polarized feeds). The wide bandwidth of the CARMA correlator allowed us to observe both the ¹²CO($J = 1 \rightarrow 0$) and the ¹³CO($J = 1 \rightarrow 0$) lines simultaneously. The ¹²CO (¹³CO) line was observed with five (three) overlapping 500 MHz bands, covering \approx 7000 (5000) km s⁻¹ total, at 42 km s⁻¹ resolution, with 3-bit sampling. These observations were carried out from August to November 2011 in CARMA's D configuration, with 11 - 150 m baselines yielding a typical synthesized beam of $4.8'' \times 3.9''$ at 88 GHz. Each galaxy was observed for 20 to 30 hours (time on-source) in moderate to good weather conditions for 3mm observation, vielding final images with rms noise of $\approx 1.2 \text{ mJy beam}^{-1}$ in a 42 km s⁻¹ channel. The flux scale in each dataset is set by the flux of the phase calibrator, which is determined from the flux calibrator. For these data, we use phase calibrators 0854+201 (4 Jv. 9% linearly polarized). 1357+193 (0.8 Jy) and 1310+323 (1.7 Jy).

All four galaxies were clearly detected in the $\operatorname{CO}(J = 1 \to 0)$ line, as shown in Figure 3. The top panels show the vector-averaged *Real* and *Imaginary* amplitudes and phase of the calibrated uv data versus velocity for the $\operatorname{CO}(J = 1 \to 0)$ line. For a compact source at the center of the field of view, the *Real* part shows the signal without a noise bias, and the *Imaginary* part shows the noise. In all four cases, we see coherent emission (larger *Real amplitudes* coincident with noise-like *Imaginary* amplitudes and phases of ≈ 0) over multiple velocity channels, indicative of a detection. We report no detection of the ${}^{13}\operatorname{CO}(J = 1 \to 0)$ line, which is expected to be weaker than the ${}^{12}\operatorname{CO}(J = 1 \to 0)$ line by a factor of 7 to 17 (Rickard & Blitz 1985).

3.2. $CO(J = 3 \rightarrow 2)$

The CO($J = 3 \rightarrow 2$) transition at the redshift of the galaxies discussed here lies in the CARMA 1 mm band (dual-polarization, circularly polarized feeds). We again observed both the ¹²CO($J = 3 \rightarrow 2$) and the ¹³CO($J = 3 \rightarrow 2$) lines simultaneously. The ¹²CO (¹³CO) line was observed with three (one) overlapping 500 MHz bands, covering ≈ 1500 (550) km s⁻¹ total, at 14 km s⁻¹ resolution, with 3-bit sampling. These observations were carried out in CARMA's E and D configuration during August 2011 and April 2012, respectively. Source C4 was observed entirely in E configuration, while

³ http://carma.astro.umd.edu/wiki/index.php/EGN



Figure 3. Vector-averaged Real (solid) and Imaginary (dotted) amplitudes (Real,Imag in mJy beam⁻¹) and phase (ph, degrees) of the calibrated uv data versus velocity (km s⁻¹) for the $CO(J = 1 \rightarrow 0)$ (red, top panel) and $CO(J = 3 \rightarrow 2)$ (blue, bottom panel) transitions in each of the four sources (indicated in upper left corner). With the higher resolution of the $CO(J = 3 \rightarrow 2)$ data, we observe the peak of the $CO(J = 3 \rightarrow 2)$ emission to be offset (< 1.5" ~ 6 kpc) from the centers of galaxies C1 and C2. In these cases, we calculate the uv spectra at the peak of the $CO(J = 3 \rightarrow 2)$ emission. For the $CO(J = 1 \rightarrow 0)$ line of galaxy C1, we average 2 channels together in order to increase the signal to noise ratio. Large Real amplitudes (the Imaginary part shows the noise) coincident with phases of ≈ 0 over multiple velocity channels indicate a detection.

the other three sources were observed mostly in D configuration. The E configuration has 8-66 m baselines yielding a typical synthesized beam of $3.2'' \times 2.5''$ at 266 GHz. The D configuration has 11-150 m baselines yielding a typical synthesized beam of $1.7'' \times 1.5''$ at 266 GHz. Each galaxy was observed for 2 to 6.5 hours (time on-source) in good weather conditions for 1mm observation, yielding final images with rms noise of 5-10 mJy beam⁻¹ in a 42 km s⁻¹ channel. For these data, we use phase calibrators 0854+201 (2 Jy in August 2011, 4 Jy in April 2012), 1224+213 (0.6 Jy) and 1310+323 (0.6 Jy).

Sources C2, C3 and C4 were detected at the $\approx 5\sigma$ level in the CO($J = 3 \rightarrow 2$) line. However, C1, with its wide velocity profile (observed in the CO($J = 1 \rightarrow 0$) line), was only marginally detected and we give only an upper limit on the CO($J = 3 \rightarrow 2$) flux. The vectoraveraged *Real* and *Imaginary* amplitudes and phase of the calibrated uv data versus velocity for the CO($J = 3 \rightarrow 2$) line are shown in the bottom panels of Figure 3. The peak of the CO($J = 3 \rightarrow 2$) emission in galaxies C1 and C2 is offset from the nominal center of each galaxy, so the uv spectra are calculated at this slightly offset (< 1.5" ~ 6 kpc)) position. We report no detection in the ¹³CO($J = 3 \rightarrow 2$) line for any galaxy.

3.2.1. Source C1 Upper Limit

Due to the wide integrated velocity profile of source C1, the $CO(J = 3 \rightarrow 2)$ line was only marginally detected. The channel maps did not show evidence of a source upon visual inspection, but an integrated spectrum made of a circular region 4.5'' in radius at the center of the image suggests a 3σ detection. The line flux and other quantities are calculated from this spectrum, over the velocities of the $CO(J = 1 \rightarrow 0)$ line for this galaxy. These values should be taken as an upper

limit on the true flux. The error in the flux measurement $(S_{\rm CO}, \, {\rm Jy\,km\,s^{-1}})$ is calculated from the pixel noise, $\sigma_{\rm p}$ (Jy beam⁻¹): $\sigma_{S_{\rm CO}} = \sigma_{\rm p} \, \delta V \sqrt{N_{\rm p}/N_{\rm eq}}$ where δV is the channel width (km s⁻¹), $N_{\rm p}$ is the number of pixels summed and $N_{\rm eq}$ is the number of pixels equivalent to the beam.

3.3. Derived Properties of the CO Emission

Table 2 presents the quantities we derive from the CO emission images. The CO line luminosity is calculated from the line flux ($S_{\rm CO}$ in Jy km s⁻¹, calculated as described in Section A.2) following

$$L'_{\rm CO} = 3.25 \times 10^7 \ S_{\rm CO} \ \nu_{\rm obs}^{-2} \ r_{\rm com}^2 (1+z)^{-1} \qquad (2)$$

(see the review by Solomon & Vanden Bout 2005), where $\nu_{\rm obs}$ is in GHz and $r_{\rm com}$ is the comoving distance in Mpc. The units of $L'_{\rm CO}$ are K km s⁻¹ pc². We report the measurement error for $S_{\rm CO}$. The error reported for $L'_{\rm CO}$ includes both the measurement error of $S_{\rm CO}$ and a 30% systematic error, added in quadrature (see Section A.2 for more details).

The center velocity, v_{center} , is the flux-weighted average velocity of the galaxy-integrated spectrum (v = 0at the redshift in Table 1). The error reported is the standard deviation of the v_{center} values found with the three flux measurement methods and different channel averaging described in Section A.2. The reported velocity width (ΔV) is the full width of the emission, where 'source' velocity channels are selected by eye. We give the velocity width of a single channel as the error. The line ratio r_{31} is given by

$$r_{31} = L'_{\rm CO(3-2)} / L'_{\rm CO(1-0)} \tag{3}$$

and the error is calculated by propagating the errors of the individual line luminosities.

Name	Transition	$S_{\rm CO}$	$L'_{\rm CO}$	v_{center}	ΔV	Non-matched r_{31}^b
		$(Jy \text{ km s}^{-1})$	$(10^9 \text{ K km s}^{-1} \text{ pc}^2)$	$({\rm km \ s^{-1}})$	$({\rm km \ s^{-1}})$	01
C1	$CO(J = 1 \rightarrow 0)$	2.05 ± 0.34	8.25 ± 2.83	-84.9 ± 18.1	542.2 ± 41.7	$0.49^{a} \pm 0.26$
	$CO(J = 3 \rightarrow 2)$	$9.02^{a} \pm 2.65$	$4.03^{a} \pm 1.69$	$-49.9\pm$ 7.3	542.3 ± 23.4	
C2	$CO(J = 1 \rightarrow 0)$	2.35 ± 0.10	10.70 ± 3.24	$-6.7\pm$ 1.2	253.7 ± 42.3	0.40 ± 0.18
	$CO(J = 3 \rightarrow 2)$	8.39 ± 1.12	4.25 ± 1.40	$19.5\pm$ 8.2	169.2 ± 42.3	
C3	$CO(J = 1 \rightarrow 0)$	4.39 ± 0.09	21.70 ± 6.53	$-24.7\pm$ 5.7	384.0 ± 42.3	0.34 ± 0.15
	$CO(J = 3 \rightarrow 2)$	13.46 ± 1.56	7.39 ± 2.38	$-14.0\pm$ 7.8	426.7 ± 42.7	
C4	$CO(J = 1 \rightarrow 0)$	3.01 ± 0.11	12.30 ± 3.72	17.3 ± 13.0	292.5 ± 41.8	0.44 ± 0.19
	$CO(J = 3 \rightarrow 2)$	11.88 ± 1.22	5.41 ± 1.72	33.5 ± 5.0	250.7 ± 41.8	

Table 2

Properties of the CO emission (described in Section 3.3). For each galaxy, the CO line flux ($S_{\rm CO}$), luminosity ($L'_{\rm CO}$, see Equation 2), central velocity (v_{center}) and full velocity width (ΔV) are given for the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ lines. The ratio of the line luminosities (r_{31}) for each galaxy is given in the last column. ^{*a*} CO $(J = 3 \rightarrow 2)$ values for source C1 are upper limits.

 b r_{31} reported here is calculated from the total line luminosities (see Section 4.1). We perform a more careful calculation, matching the 1 and 3mm data, in Section 4.3.

Moment maps (discussed in Section 4.2 and displayed in Appendix B) are created from the 2σ clip smooth mask (see Section A.2). Moment 0 (total intensity) maps are a simple sum of the masked images in the 'source' velocity channels. Moment 1 (intensity-weighted mean velocity) maps are produced by summing the masked image multiplied by the velocity in each channel then normalizing by the moment 0 value.

4. ANALYSIS

We first present our total r_{31} measurements (using the total flux observed in each line) in Section 4.1. All four observed galaxies are discussed. However, the total r_{31} values use line luminosities calculated completely independently of one another, making no attempt at matching the spectral or spatial resolution. In Section 4.2, we carefully match the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ data to each other as well as possible, in both spectral and spatial resolution. In Section 4.3 we re-calculate r_{31} using both the natural and adjusted spatial resolution, with matched spectral resolution in both cases. In Section 4.4 we investigate the radial dependence of r_{31} by fitting two-dimensional Gaussians to the total intensity maps in order to derive peak intensities, which are independent of spatial resolution. The analysis in Sections 4.2-4.4 is performed only for the three galaxies that are detected significantly in both lines (C1 is excluded due to marginal detection of the $CO(J = 3 \rightarrow 2)$ line).

4.1. Total r_{31}

As a first step, we calculate r_{31} in the simplest way possible, taking the ratio of the total line luminosities. Of the four galaxies observed, we detect three in both lines, yielding r_{31} values (see Table 2) of 0.34 to 0.44 with an average value of 0.39. For source C1 we derive an upper limit on r_{31} of 0.49, which is consistent with the other values.

These r_{31} values carry the caveat that they are determined from line luminosities that are calculated independently of one another. The 'source' velocity channels for each line are selected by eye for the most convincing detection. Further, the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ lines are observed at different frequencies in the same configuration (except source C4). This yields different sampling of the *uv*-plane, which means that the two maps are sensitive to slightly different spatial scales. We re-calculate r_{31} more carefully for C2, C3 and C4 in the following sections.

4.2. Matching the 1 and 3 mm Data

In this section, we attempt to standardize the flux calculated for each line as much as possible by matching both spatial and spectral resolution. First, we use the same spectral resolution in both the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ data, selecting the starting channel so that the image velocity channels line up exactly.

Next, to investigate the effect of the different uv sampling of the two lines, we re-create the images using only data at uv distances present in both the 1 and 3 mm data (matched uv data): 8-44 k λ , which corresponds to spatial scales of $\approx 2.5''$ -13''. Further, we force all the images to have a standard pixel size (0.99'' for all except the $CO(J = 3 \rightarrow 2)$ line for C2 and C3 using all uv data, for which we use 0.33'' pixels since these images have higher resolution). Figures 8 - 10 in Appendix B show images and spectra calculated within the standard source regions (discussed in Section A.2) using all uv data (top panel) and using matched uv data (bottom panel).

This *uv*-distance restriction makes the beam sizes more similar, but not necessarily the same due to different sampling within the allowed *uv*-distance range. Table 3 compares the measured fluxes and beam sizes using all uv data and matched uv data. The change in the measured flux is $\leq 6\%$ for sources C2 and C4, which is less than the expected measurement error in the total flux. However, the change in flux is more significant for source C3 in both lines. For the $CO(J = 1 \rightarrow 0)$ line, the matched *uv*-coverage excludes the short *uv* spacings, which are sensitive to large-scale structure. Therefore, the presence of extended emission in source C3 would explain the decrease in flux in the matched *uv* data. This is

Name,	All uv data		Mat	Flux	
Trans.	$S_{\rm CO}$	Beam	$S_{\rm CO}$	Beam	% Diff.
C2 1-0	2.30	$4.90'' \times 4.08''$	2.15	$4.54'' \times 3.75''$	-6.5%
3-2	7.06	$1.70'' \times 1.56''$	7.00	$3.20'' \times 2.84''$	-0.8%
C3 1-0	4.29	$4.97'' \times 4.06''$	3.71	$4.62'' \times 3.77''$	-13.5%
3-2	13.75	$1.71^{\prime\prime} \times 1.46^{\prime\prime}$	11.61	$3.12^{\prime\prime} \times 3.02^{\prime\prime}$	-15.6%
C4 1-0	2.95	$4.99'' \times 4.02''$	2.76	$4.62'' \times 3.83''$	-6.4%
3-2	12.79	$3.33^{\prime\prime} \times 2.41^{\prime\prime}$	12.01	$3.55^{\prime\prime} \times 3.08^{\prime\prime}$	-6.1%

Table 3

Comparison of uv data selections. Measured CO line fluxes ($S_{\rm CO}$ in Jy km s⁻¹) and beam sizes for images made using all uv data and matched uv data. The fluxes reported here are calculated using the 2σ smooth masking technique discussed in Section A.2.

The percent difference in the measured flux is defined as $100(S_{\rm CO,match} - S_{\rm CO,all})/S_{\rm CO,all}$.



Figure 4. $L'_{\rm CO}$ and r_{31} profiles for the three detected sources. The top panels show the $L'_{\rm CO}$ profiles for the ${\rm CO}(J = 1 \rightarrow 0)$ (red) and ${\rm CO}(J = 3 \rightarrow 2)$ (blue) transitions using all uv data (all uv, solid lines) and matched uv data (mat uv, dashed lines). The shading under each profile indicates which velocity channels are considered part of the source emission for each transition. The r_{31} profile is plotted in the bottom panel for both uv selections (all uv in solid black, matched uv in dashed magenta). The average r_{31} value for each profile is plotted as a horizontal black dotted (all uv data) or magenta dash-dotted (matched uv data) line.

supported by the radial profile of the $\operatorname{CO}(J = 1 \to 0)$ cumulative flux in Figure 6 in Appendix A, which shows the matched uv data agreeing with the all uv data at small radii and diverging at larger radii. The $\operatorname{CO}(J = 3 \to 2)$ line, on the other hand, looses long uv spacings (sensitive to small-scale structure) in the matched uv data. However, the uv-distance restriction excludes a sizeable fraction of the uv data, which decreases the signal to noise in the image so that less flux is recovered using the masking technique. A comparison of the unmasked $\operatorname{CO}(J = 3 \to 2)$ line fluxes in the all uv and matched uv datasets for source C3 shows a drop of only 7.2%, which is within the expected measurement error.

In the rest of our analysis, we consider the emission measured in both cases of uv coverage.

4.3. Integrated r_{31} Velocity Profiles

We now make a more careful measurement of r_{31} , with the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ flux measurements as well-matched to one another as possible. For each uv data selection (all uv, matched uv), we calculate r_{31} in each channel where flux is measured in both lines. Figure 4 shows the integrated L'_{CO} and r_{31} velocity

Figure 4 shows the integrated $L'_{\rm CO}$ and r_{31} velocity profiles for each of the three significantly detected galaxies. $L'_{\rm CO}$ as a function of velocity is plotted in the top panels for each transition (CO($J = 1 \rightarrow 0$) in red, CO($J = 3 \rightarrow 2$) in blue), for all uv data (solid lines) and matched uv data (dashed lines). Source velocity channels for each line (chosen by eye) are indicated by shading in the corresponding color. The bottom panels show the r_{31} profiles for all uv data (solid black line, with the average value indicated by the horizontal black dotted line) and the matched uv data (dashed magenta line, with average value shown by the horizontal magenta dash-dotted line). For galaxy C2, we have excluded the velocity channels at $\pm 86 \text{ km s}^{-1}$ from this analysis. At -86 km s^{-1} , we do not detect the CO($J = 3 \rightarrow 2$) line despite a 3σ detection in the CO($J = 1 \rightarrow 0$) line. At $+86 \text{ km s}^{-1}$, the CO($J = 3 \rightarrow 2$) image suggests a weak (2σ) detection at the center, but the measured flux is dominated by a 3σ noise spike close to this emission. Therefore, we use only the central three velocity channels in the CO($J = 3 \rightarrow 2$) transition.

In galaxies C2 and C3, the r_{31} profiles appear well behaved, remaining roughly constant in all velocity channels. On the other hand, galaxy C4 shows significant deviations from a flat profile, with a very low r_{31} at ≈ 0 km s⁻¹ and a very high value at ≈ 40 km s⁻¹. Due to the modest signal to noise ratio at which the CO($J = 3 \rightarrow 2$) line is detected in each channel, we cannot draw any definitive conclusions, but note that if the enhanced r_{31} is real, it may indicate a region of enhanced gas excitation (at a velocity close to 0, it is likely to be physically near the center of the galaxy), such as a starbursting clump, in which a higher r_{31} would be expected.

For each galaxy, Table 4 gives the number of velocity channels in which r_{31} is calculated, the mean and standard deviation (σ) of r_{31} for each uv data selection and the the average r_{31} value for the two uv data selections (galaxy mean), with the expected measurement error (meas. error). We expect a 20% measurement error in the flux of each line, in each channel (Section A.2), which gives a 30% error in r_{31} in each channel, and a $30\%(N_{\rm ch})^{-1/2}$ error in the average r_{31} . This value is reported in the last column of Table 4 for each galaxy. The bottom rows give the mean and standard deviation of the

	Name	$N_{\rm ch}$	All uv		Matched uv		Galaxy	Meas.
l			Mean	σ	Mean	σ	Mean	Error
ſ	C2	3	0.45	0.06	0.47	0.14	0.46	0.08
	C3	8	0.39	0.12	0.39	0.14	0.39	0.04
	C4	6	0.54	0.32	0.50	0.32	0.52	0.06
ſ			Mean	0.46				
l			ple σ	0.07				

Table 4

Summary of EGNoG galaxy r_{31} values. For each source, we give the number of velocity channels in which r_{31} is calculated $(N_{\rm ch})$, the mean and standard deviation (σ) of r_{31} using all uv data and the matched uv data, and the average r_{31} value for each galaxy, with the expected measurement error. In the bottom rows we give the mean and standard deviation of r_{31} in this sample of three galaxies. The expected measurement error for the average

 r_{31} in each galaxy is the expected measurement error in each channel (30%) divided by $\sqrt{N_{\rm ch}}$.

average r_{31} values for the three sample galaxies. In this paper, the standard deviation given is the square root of the unbiased sample variance.

The average values for each uv selection are consistent with each other within each galaxy and roughly consistent across the three galaxies. While the uv selection appears to have a small effect on the average r_{31} value, it is not in a systematic direction. The standard deviation of r_{31} we observe in galaxies C2 and C3 is consistent with the expected 30% measurement errors in each channel. The standard deviation for galaxy C4 is roughly twice the expected 30% error due to the two outlier channels discussed above. Overall, in the three EGNoG galaxies discussed here, we find a mean r_{31} of 0.46 with a standard deviation of 0.07. Since we estimate each line flux has systematic errors of of up to $\approx 30\%$ (see Section A.2), the systematic errors in the ratio r_{31} will be $\leq 40\%$.

4.4. Radial Dependence of r_{31}

Since r_{31} traces the local excitation conditions of the molecular gas of a galaxy, it is expected to vary within the disk of the galaxy. In fact, Dumke et al. (2001) found $CO(J = 3 \rightarrow 2)$ emission to be more centrally concentrated than $CO(J = 1 \rightarrow 0)$ emission in nearby galaxies, so that r_{31} decreased with radius. To look for radial variation in r_{31} in the EGNoG data, we cannot compare the emission maps directly due to the marginal resolution of the galaxies and the different uv coverage of the two transitions. In order to disentangle the true emission distribution from the uv sampling, we fit a two-dimensional Gaussian to the total intensity (moment 0) map of each CO transition using the MIRIAD program imfit. This analysis is presented in detail in Appendix C.

While the error bars are large, we do find the ratio of the deconvolved peak intensities (representative of the conditions in the central region of the galaxy) to be systematically higher than the ratio of the total fluxes. In our sample, we find $r_{31}(\text{peak}) = 0.73 \pm 0.31$, with a standard deviation across the three galaxies of 0.04. We compare this to the ratio calculated from the fit total fluxes: 0.42 ± 0.11 , with a standard deviation of 0.04. While the small standard deviations in our r_{31} values show consistency between the three galaxies, these results are plagued by sizable uncertainties as a result of fitting data with only modest signal to noise (note that our error estimates are conservative and may in fact be over-estimating the true error). Therefore, we conclude (but not robustly) that r_{31} is higher in the center of the EGNoG galaxies than in the molecular disk as a whole (consistent with Dumke et al. 2001).

5. DISCUSSION

The observed r_{31} is a function of many parameters, including the excitation temperature $(T_{\rm ex})$, optical depth (τ_{ν}) and filling factor of each line (e.g. Hurt et al. 1993). For each line, the rest-frame intensity is

$$I_{\nu} = \eta_{\rm f} \left(1 - \exp^{-\tau_{\nu}} \right) \left[B_{\nu}(T_{\rm ex}) - B_{\nu}(T_{\rm CMB}) \right] \qquad (4)$$
$$\equiv B_{\nu}(T_{\rm b}) \equiv \frac{2k\nu^2 T_{\rm b,RJ}}{c^2}$$

where $B_{\nu}(T)$ is the specific intensity of a blackbody at temperature T, $T_{\rm b}$ is the brightness temperature of the line, $T_{\rm b,RJ}$ is the Rayleigh-Jeans definition brightness temperature of the line and $\eta_{\rm f}$ is the efficiency of the coupling between the beam and source emission, which is determined by the beam size, the molecular gas disk size and the fraction of the disk that is emitting in the line (the filling factor). Note that Equation 4 is in the rest frame. The observed line intensity would be redshifted so that the corresponding observed brightness temperature (for both definitions) is reduced by a factor of (1 + z).

For equal velocity widths in both lines (as we have enforced in Sections 4.3 and 4.4), r_{31} , as defined in Equations 2 and 3, reduces to the ratio of the Rayleigh-Jeans brightness temperatures. Following Equation 4, we can write r_{31} as

$$r_{31} = \frac{T_{\rm b,RJ}(3-2)}{T_{\rm b,RJ}(1-0)} = \frac{[\eta_{\rm RJ}\eta_{\rm f}\eta_{\tau}\eta_{\rm CMB}T_{\rm ex}]_{(3-2)}}{[\eta_{\rm RJ}\eta_{\rm f}\eta_{\tau}\eta_{\rm CMB}T_{\rm ex}]_{(1-0)}}$$
(5)

where each term in Equation 4 is represented as a correction factor η so that we can express r_{31} more directly in terms of the line excitation temperatures. Specifically, $\eta_{\rm CMB}$ gives the correction from $T_{\rm ex}$ to the effective excitation temperature $(T_{\text{ex,eff}}, \text{ where } B_{\nu}(T_{\text{ex,eff}}) =$ $B_{\nu}(T_{\rm ex}) - B_{\nu}(T_{\rm CMB})$) due to the CMB term. At z = 0.3, the temperature of the cosmic microwave background $(T_{\rm CMB})$ is ≈ 3.5 K, so that for $T_{\rm ex} = 10$ - 30 K, $\eta_{\rm CMB} \approx$ 0.85 - 0.95 for the CO $(J = 1 \rightarrow 0)$ line and 0.98 - 1.00 for the $CO(J = 3 \rightarrow 2)$ line. The term accounting for the optical depth of each line is $\eta_{\tau} = (1 - e^{-\tau_{\nu}})$. The filling factor term, $\eta_{\rm f}$ (defined above) is expected to be < 1 and may be different for the two lines. Finally, we represent the difference between $T_{\rm b}$ and $T_{\rm b,RJ}$ by $\eta_{\rm RJ}$, which, for $T_{\rm b} = 10 - 30$ K, is 0.75 - 0.91 for the $CO(J = 1 \to 0)$ line and 0.39 - 0.75 for the $CO(J = 3 \rightarrow 2)$ line. Therefore, for $T_{\rm ex} = 10$ - 30 K for each line, we expect

$$r_{31} = (0.4 - 1.2) \frac{|\eta_{\rm f} \eta_{\tau} T_{\rm ex}|_{3-2}}{[\eta_{\rm f} \eta_{\tau} T_{\rm ex}]_{1-0}} \tag{6}$$

The excitation temperature of a given emission line will fall between the radiation temperature ($T_{\rm CMB}$) and the kinetic temperature, depending on the density of the gas. Where the molecular gas density is larger than the critical density (for 20 K gas, $n_{\rm crit} \approx 10^3 \text{ cm}^{-3}$ for ${\rm CO}(J = 1 \rightarrow 0)$ and $\approx 10^5 \text{ cm}^{-3}$ for ${\rm CO}(J = 3 \rightarrow 2)$), the excitation temperature is equal to the kinetic temperature of the gas. Thus we see that optically thick gas with equal excitation temperature in both lines will have $r_{31} \approx 1.0 \pm 0.5$ for $T_{\rm ex} \approx 10 - 30$ K (depending on

the relative filling factors and optical depths of the two lines). This is consistent with the general criterion that gas with $r_{31} < 1$ is sub-thermal and $r_{31} > 1$ is thermalized. Note that deviation from $r_{31} = 1$ in thermalized gas is a strong function of excitation temperature (due to $\eta_{\rm CMB}$ and $\eta_{\rm RJ}$): higher excitation temperature gas will have r_{31} closer to unity when thermalized. More generally, if one considers various optical depths (assuming local thermodynamic equilibrium (LTE) with equal excitation temperatures), r_{31} greater than unity is indicative of warm, optically thin gas and a ratio less than unity is indicative of optically thick gas (e.g. Meier et al. 2001).

Therefore, while we can comment on whether the excitation of the CO $J_{\rm upper}$ state is likely to be sub-thermal or thermalized, determining the conditions of the gas more accurately requires modeling of multiple transitions (e.g. using Large Velocity Gradient (LVG) models). Since one line ratio does not provide strong constraints, we do not perform LVG modeling as part of this work. In the following sections we compare the r_{31} values found in the EGNoG galaxies to previous studies at low and high redshift and we discuss the implications of this work for the interpretation of CO measurements in intermediate and high redshift galaxies.

5.1. Comparison with Previous Work

To date, the study of CO line ratios in intermediate and high redshift galaxies has been dominated by work on extreme starbursting systems: SMGs and quasars. The CO lines from $(J = 1 \rightarrow 0)$ up to $(J = 9 \rightarrow 8)$ in quasars at $z \approx 2-4$ are well-fit by a single component of highly excited gas (Riechers et al. 2006; Weiß et al. 2007; Riechers 2011). In contrast, while the high-J CO transitions in $z \approx 2-4$ SMGs are fit by similar highly excited gas, recent observations of the $CO(J = 1 \rightarrow 0)$ line in these systems reveal a diffuse, low-excitation component in addition to the highly excited component (Carilli et al. 2010; Riechers et al. 2011), similar to what has been observed in local ULIRGS (Papadopoulos et al. 2007; Greve et al. 2009). In contrast, the limited work on $z \approx 1-2$ SFGs suggests low-excitation gas similar to the Milky Way (Dannerbauer et al. 2009; Aravena et al. 2010). Since the EGNoG galaxies are SFGs (lying on the main sequence), we restrict the rest of this discussion to SFGs (normal star-forming galaxies) at low and high redshift.

To place the r_{31} values we measure at $z \approx 0.3$ in the context of previous work on normal SFGs, Figure 5 shows r_{31} versus approximate SFR for the EGNoG galaxies (red diamonds) and a compilation of literature data, which includes three large surveys of r_{31} in nearby galaxies (Yao et al. 2003; Mao et al. 2010; Papadopoulos et al. 2011) as well as the study at z = 1.5 (Aravena et al. 2010). We plot r_{31} from our matched analysis (Section 4.3) for sources C2, C3 and C4 (values from Table 4, with 40% error bars to indicate potential systematic errors) and the upper limit for source C1 derived from the total line luminosities (Section 4.1, Table 2). While SFRs are available for the present survey and Aravena et al. (2010), the other three surveys only provide total infrared luminosities $(L_{\rm IR})$ or far infrared luminosities $(L_{\rm FIR})$ calculated from IRAS (the Infrared Astronomical Satellite) fluxes. We use approximate SFRs of $1.7 \times 10^{-10} L_{\rm FIR} M_{\odot}$ yr⁻¹ ($L_{\rm FIR}$ in L_{\odot}; Kennicutt 1998) and $LIR/L_{\rm FIR} = 1.3$ (Graciá-Carpio et al. 2008) in Figure 5. Values for the



Figure 5. Compilation of r_{31} literature data. r_{31} is plotted against approximate SFR $(1.7 \times 10^{-10} L_{\rm FIR}$ when a SFR is not available) for the following datasets: Yao et al. (2003) (Yao03), Mao et al. (2010) (Mao10), Papadopoulos et al. (2011) (Papa11), Aravena et al. (2010) (Arav10), this paper (EGNoG) and Fixsen et al. (1999) (MW GC, inner and outer). Milky Way points are shown at the left side of the plot for clarity. The black horizontal dashed line shows $r_{31} = 1$ and the horizontal solid lines indicate the average values for Yao03, Mao10 and Papa11 (the corresponding shaded rectangles show the standard deviation around the average values).

Milky Way are plotted as well: the galactic center (MW GC), inner disk (MWinner), and outer disk (MWouter) values, all in black, are taken from Fixsen et al. (1999) and plotted (slightly offset from one another) for illustrative purposes at the left side of the plot. The average r_{31} values of the Yao et al. (2003), Mao et al. (2010) and Papadopoulos et al. (2011) datasets are indicated by the horizontal lines of the corresponding color, with the corresponding shaded rectangles indicating the standard deviation around the average values. To guide the eye, the black dashed line shows $r_{31} = 1$.

Despite the large range of values observed, we find general agreement between our values, that of Aravena et al. (2010) and the average values of the local surveys, with the EGNoG galaxies showing slightly lower r_{31} values than the other studies. Note that the Mao et al. (2010)survey found an average value of 0.81 for the entire sample, but a lower average of 0.61 for galaxies classified as 'normal', based on SFR surface density as indicated by the far infrared luminosity and optical diameter. Further, the $CO(J = 3 \rightarrow 2)$ survey of local, low-SFR spirals by Wilson et al. (2012) find a lower value (using $CO(J = 1 \rightarrow 0)$ luminosities from Kuno et al. 2007) of $r_{31} \approx 0.2$, but note that the authors have not made any correction for differences in the fraction of each galaxy mapped by the two surveys. Their r_{31} value is at the low end of the spread of values plotted in Figure 5. The range and average r_{31} values for the points plotted (including number of galaxies, redshift and SFR ranges) are given in Table 5.

	Dataset	Ν	Redshift	SFR ¹	r_{31}	
			Range	$(M_{\odot} \text{ yr}^{-1})$	Range	Mean
	Milky Way	3			0.4 - 0.9	0.68
	Mao 2010	61	0.0 - 0.04	0.03 - 200	0.2 - 1.9	0.81
	normal	7			0.3 - 1.5	0.61
	starburst	25			0.3 - 1.9	0.89
	Yao 2003	60	0.007 - 0.05	0.1 - 100	0.2 - 1.7	0.66
	Papa 2011	70	0.006 - 0.08	0.7 - 150	0.1 - 1.9	0.67
	EGNoG	3	0.28 - 0.31	39 - 65	0.39 - 0.52	0.46
-	Arav 2010	1	1.52	220		0.61

Table 5

Summary of r_{31} from the literature. The range and mean values are given for the following datasets: Fixsen et al. (1999) (Milky Way), Mao et al. (2010) (Mao 2010), Yao et al. (2003) (Yao 2003), Papadopoulos et al. (2011) (Papa 2011), this paper (EGNoG) and Aravena et al. (2010) (Arav 2010). Columns 2 to 4 give the number of galaxies, redshift and SFR ranges for each dataset. For Mao 2010, we also report the r_{31} range and average for the 'normal' and 'starburst' subsets.

 1 SFR values are approximate (see Section 5.1).

In order to compare our values to the literature data, we first discuss the nature of the observations presented. Yao et al. (2003) observe 60 IR-luminous galaxies (most sources have $L_{\rm FIR} > 10^{10} L_{\odot}$) selected from the SCUBA Local Universe Galaxy Survey (SLUGS). Each line is measured with a single pointing of a single-dish telescope: $CO(J = 1 \rightarrow 0)$ at the Nobeyama Radio Observatory (NRO), $CO(J = 3 \rightarrow 2)$ at the James Clerk Maxwell Telescope (JCMT). For both measurements, the beam size is $\approx 15''$, corresponding to physical sizes of $\approx 0.5-13$ kpc for their sample galaxies ($\approx 0.5-5$ kpc for most of the sample).

Mao et al. (2010) measure the $\operatorname{CO}(J = 3 \rightarrow 2)$ line for 125 nearby galaxies of various types (e.g. normal, starburst, LIRG, ULIRG) using the Heinrich Hertz Telescope (HHT; beam size $\approx 22''$). This beam size corresponds to a physical size of $\approx 0.25 - 17$ kpc for the sample galaxies (1.7 kpc on average). The $\operatorname{CO}(J = 1 \rightarrow 0)$ data for their sample were taken from the literature and therefore the beam size depends on the telescope used. In their analysis, Mao et al. (2010) only use those galaxies for which they found IRAM 30m $\operatorname{CO}(J = 1 \rightarrow 0)$ data (61), which have a beam size matching the HHT $\operatorname{CO}(J = 3 \rightarrow 2)$ data. These measurements are plotted with error bars in Figure 5. Galaxies with $\operatorname{CO}(J = 1 \rightarrow 0)$ data from other sources are reported as upper or lower limits.

Papadopoulos et al. (2011) examine a composite sample of 70 LIRGs in the nearby universe ($z \leq 0.1$) spanning a wide range of morphologies. They present new measurements of 36 galaxies and data from the literature for 34 more. The new measurements use the IRAM 30m telescope for $CO(J = 1 \rightarrow 0)$ (beam size $\approx 22''$) and the JCMT for $CO(J = 3 \rightarrow 2)$ (beam size $\approx 14''$), and therefore are not observed with the same beam size. The authors do not comment on matching beam sizes in the new measurements or those from the literature.

The galaxy in which Aravena et al. (2010) measure r_{31} , BzK-21000 at z = 1.5, was observed in the CO($J = 3 \rightarrow 2$) line with the Plateau de Bure Interferometer (PdBI) by Dannerbauer et al. (2009) and in the CO($J = 1 \rightarrow 0$) line with the Very Large Array (VLA) in C and D configurations (Aravena et al. 2010). In both cases, the source is unresolved or marginally resolved, so the measured fluxes should represent the total emission of the galaxy.

The three samples of nearby galaxies are observed with single-dish instruments, typically sampling the inner portion of the molecular gas disk of the observed galaxies. This is different from the r_{31} measurements for the EGNoG galaxies (Table 4) and the galaxy at z = 1.5 (Aravena et al. 2010), for which the emission from the entire gas disk is observed. We note that a gradient in r_{31} has been observed in nearby galaxies (Dumke et al. 2001), with higher values measured in the centers. This can be inferred from the Milky Way measurements (Fixsen et al. 1999) as well. This effect may well account for the EGNoG and Aravena et al. (2010) measurements appearing systematically lower than the average values reported by the surveys observing the central regions of nearby galaxies. Supporting this explanation, our analysis in Section 4.4 suggests r_{31} is higher in the centers of the EGNoG galaxies (more in line with the average values of the local surveys) compared to r_{31} averaged over the entire disk. However, with such a large spread in values and inhomogeneous datasets, it is difficult to draw any robust conclusions on this point.

5.2. Implications

We have measured $r_{31} = 0.46 \pm 0.07$ (with systematic errors of up to 40%) in three galaxies at $z \approx 0.3$, suggestive of optically thick, sub-thermal gas. Despite being massive and highly star-forming (with SFRs of 50-65 M_{\odot}) yr⁻¹ and stellar masses of $\approx 2 \times 10^{11}$ M_{\odot}), the excitation of the gas in these galaxies is consistent with SFGs like local spirals, not star-bursting systems like ULIRGS, SMGs and quasars. Since the EGNoG galaxies have been selected from the main sequence of star-forming galaxies at z = 0.3, our findings suggest that galaxies on the main sequence, over a range of star formation activity, harbor sub-thermally excited gas. Therefore, we suggest that CO line ratios similar to those observed in local spiral galaxies are appropriate for main-sequence star-forming galaxies.

The extension of the EGNoG results to main-sequence star-forming galaxies means that sub-thermal line ratios are appropriate for the $z \sim 1-2$ SFGs in which Tacconi et al. (2010) and Daddi et al. (2010) report high molecular gas fractions (20-80%). Tacconi et al. and Daddi et al. estimated the molecular gas mass associated with the observed $J_{upper} > 1$ CO luminosity assuming sub-thermal $r_{\rm J1}$ line ratios and a Milky Way-like $\alpha_{\rm CO}$ (Daddi et al. 2010 used a slightly smaller value for $\alpha_{\rm CO}$). As the conversion factor is a complex problem, expected to vary as a function of gas excitation, density, metallicity and radiation field (Shetty et al. 2011; Leroy et al. 2011), the results of this work do not directly inform the choice of conversion factor. However, the r_{31} line ratios of the EGNoG gas excitation sample support the assumption of a sub-thermal line ratio in these studies. Specifically, Tacconi et al. (2010) use $r_{31} = 0.5$ to calculate molecular gas masses, which is consistent with our results (Daddi et al. 2010 observed the $CO(J = 2 \rightarrow 1)$ line and assume a sub-thermal r_{21}).

6. CONCLUSIONS

This paper presents the gas excitation sample of the EGNoG survey. We report robust detections of the $CO(J = 3 \rightarrow 2)$ and $CO(J = 1 \rightarrow 0)$ lines in three galaxies at $z \approx 0.3$, and an upper limit for the fourth galaxy.

The average r_{31} value for this sample is 0.46 ± 0.07 , with systematic errors of up to 40%. This value is consistent with published r_{31} values for main-sequence star-forming galaxies at $z \approx 0$ as well as the single measurement of at z > 0.3 (Aravena et al. 2010). The sub-thermal excitation of the $CO(J = 3 \rightarrow 2)$ line suggests the excitation state of the molecular gas in these galaxies is similar to local spirals, and is not indicative of a starburst. We conclude that the galaxies in our sample (and by extension, the main sequence galaxies at $z \sim 1-2$ studied by Tacconi et al. 2010 and Daddi et al. 2010) harbor cold, optically thick molecular gas despite being massive and highly star-forming.

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APPENDIX

A. DATA REDUCTION AND FLUX MEASUREMENT

A.1. Data Reduction

Each dataset is reduced and calibrated as follows. The data are flagged for antenna - antenna shadowing as well as any other issues during the observation. The instrument bandpass is calibrated with mfcal on a bright passband calibrator. The time-dependent antenna gains (from atmospheric variation) are derived by performing a selfcal on the phase calibrator with an averaging interval of 18 minutes (the timescale of switching between the source and phase calibrator). For sources C1 and C2, the phase calibrator, 0854+201, is $\approx 10\%$ polarized, which required additional steps in the reduction of the 3mm data (observed with linearly polarized feeds). This is described in more detail in the full survey paper, Bauermeister et al. 2012b, in preparation.

For each dataset, the flux of the phase calibrator is set during the antenna gain calibration in order to properly set the flux scale of the data. The flux of each phase calibrator is assumed to be constant over timescales of weeks, and is therefore determined from the best datasets of the survey using **bootflux** on bandpass-calibrated, phase-only gain-calibrated data with Mars or MWC349 as a primary flux calibrator. The brightness temperature of Mars is set by the CARMA system using the Caltech thermal model of Mars (courtesy of Mark Gurwell), which includes seasonal variations in temperature and can be accessed in MIRIAD using **marstb**. This model gives brightness temperatures ≈ 218 K at 266 GHz and $\approx 208 - 200$ K at 88 GHz for August-November 2011 observations, and ≈ 201 K at 266 GHz for April 2012 observations. For MWC349 we set the flux to 1.2 Jy at 88 GHz, the typical value from historical flux monitoring at CARMA. The fluxes used for each phase calibrator are as follows: for the 3mm data (≈ 89 GHz, August to November 2010), the flux of 0854+201 is set to 4 Jy (9% linearly polarized), 1357+193 0.8 Jy and 1310+323 1.7 Jy. For the 1mm data (≈ 265 GHz, August 2011 and April 2012) the flux of 0854+201 is set to 2 Jy in August 2011 and 4 Jy in April 2012, 1224+213 0.6 Jy in April 2012 and 1310+323 0.6 Jy in August 2011.

Images are produced combining all fully calibrated datasets for each source. We used **invert**, weighting the visibilities by the system temperature as well as using a Briggs' visibility weighting robustness parameter (Briggs 1995) of 0.5. Since CARMA is an inhomogeneous array (these data use both the 10m and 6m dishes), we also use options=mosaic in the **invert** step in order to properly handle the three different primary beams patterns (10m-10m, 10m-6m and 6m-6m). All observations are single-pointing. The resulting images are primary-beam-corrected. In most of the sources discussed here, we map the 3mm data ($CO(J = 1 \rightarrow 0)$ line) channel by channel, using the full spectral resolution of 42 km s⁻¹. We match this resolution in the 1mm data ($CO(J = 3 \rightarrow 2)$ line) by averaging channels in sets of three. The exception to this scheme is source C1, which has emission spread over a very wide velocity range, requiring more channel averaging to increase the signal to noise.

We deconvolve each image with mossdi (the mosaic version of clean), cleaning down to the rms noise within a single channel, within a cleaning box selected by eye to include only source emission. We clean only channels which contain visible source emission. Cleaning down to a specified noise level is preferred to using a set number of clean iterations due to the nature of the spectral line emission: some channels will contain more flux and therefore require more clean iterations. In tests using a model source of known flux inserted into real data (emission-free channels), we found a 1σ cutoff to best extract the true source emission without overestimating the flux over a range of detection significance levels, with a 10-30% uncertainty in the recovered flux (depending on the significance of the signal). The final clean images are produced by **restor**, which convolves the clean component image with the clean beam (calculated by fitting a Gaussian to the combined mosaic beam given by mospsf), and adds the residuals from the cleaning process.

A.2. Flux Estimation

Total source fluxes in the CO lines are calculated by summing 'source' pixels in each 'source' velocity plane of the image. The source velocity planes are selected by eye. The source pixels are those within the 'source' region which are not masked by our smooth mask (adapted from Dame 2011). The smooth mask is created by applying a 2σ clip to a smoothed version of the image: Hanning smoothing is done along the velocity axis, and each velocity plane is convolved with a Gaussian beam twice the size of the original synthesized beam. This smoothed mask is used in order to exclude noise pixels but still capture low-level emission that a simple clip would miss. In our own testing (using a model source of known flux inserted into real data), we found a 2σ clip to best reproduce the true flux over a range of detection significance levels.

The appropriate source region size is selected to recover all of the flux without including the negative bowl. Since we do not have single dish data to complement the interferometric data presented here, our datasets are missing the shortest uv spacings. As a result, the emission in the clean images sits in a negative bowl, which will affect the measured flux (calculated by summing pixels within a given radius). In order to accurately estimate the flux, we use the radius at which the radial profile of the enclosed flux first peaks, thereby excluding the negative bowl. The radial profiles of the enclosed flux for sources C2, C3 and C4 are shown in Figure 6: $CO(J = 1 \rightarrow 0)$ in red in the top panels and $CO(J = 3 \rightarrow 2)$ in blue in the bottom panels. The profiles for both uv selections (all and matched), unmasked and masked are shown for each transition. The negative bowl is most evident in the unmasked profiles (dotted and dash-dotted lines), in which the enclosed flux peaks and then decreases with radius. The radius of the first peak of



Figure 6. Enclosed flux $(S_{CO} \text{ in Jy km s}^{-1})$ as a function of radius for sources C2, C3 and C4. The top panels show the $CO(J = 1 \rightarrow 0)$ line flux for four cases: all uv data, masked (solid) and unmasked (dotted); matched uv data, masked (dashed) and unmasked (dash-dotted). The bottom panels show the $CO(J = 3 \rightarrow 2)$ line flux for the same four cases. The vertical black dotted lines indicate the radius at which the enclosed flux peaks $(6.5'' \text{ for } CO(J = 1 \rightarrow 0), 4.5'' \text{ for } CO(J = 3 \rightarrow 2)$).

the enclosed flux distribution is 6.5" for the $CO(J = 1 \rightarrow 0)$ data and 4.5" for the $CO(J = 3 \rightarrow 2)$ data (shown by the vertical black dotted lines). These radii are used in the calculation of total fluxes throughout this work.

The error in the flux measurement is estimated from the standard deviation of the measured fluxes using different velocity channel averaging and starting channel, using three different methods of calculating the flux in each case. The three methods are: the 2σ masking technique described above, the same masking technique with a 3σ clip, and the simple addition of all pixels (no mask) within the source region.

We performed extensive testing of our analysis technique in order to choose the parameters of the reduction to eliminate systematic offsets and minimize the uncertainty due to noise (as described above). We find a 10-30% error in the flux measurement coming from noise in the data reduction and analysis steps. From this, we take an average uncertainty of 20% in the flux estimated in each channel, which results in a uncertainty in the total flux of $20\% (N_{\rm ch})^{-0.5}$ ($N_{\rm ch}$ is the number of velocity channels in which the flux is summed). For the total flux values reported in Table 2, we estimate the error from the variation in the flux calculated using different channel averaging, flux measurement method, etc. (described above), which is consistent with the $20\% (N_{\rm ch})^{-0.5}$ we expect. In our analysis of the integrated flux velocity profiles (Section 4.3), we assume errors of 20% in the flux in each channel.

Further, these data suffer from systematic errors due to absolute flux calibration and primary beam correction. We set the flux scale in our dataset based on a primary flux calibrator (Mars or MWC349), the flux of which is only known to $\approx 20\%$. In the primary beam correction of the dataset, pointing and focus errors at the time of the observations as well as errors in the primary beam model can significantly reduce image fidelity, leading to errors in the measured fluxes of $\approx 20\%$ (see SKA Memo #103, Wright & Corder 2008). Combining these systematic errors in quadrature, we estimate that our flux measurements suffer from systematic uncertainties of up to $\approx 30\%$. We consider all these factors in the presentation of our data in Table 2: for the line flux ($S_{\rm CO}$), we report the measured error; for $L'_{\rm CO}$, we include a 30% systematic error (added in quadrature to the measured error in $S_{\rm CO}$).



Figure 7. $CO(J = 1 \rightarrow 0)$ emission in source C1. The left panel shows the optical image. The moment 0 and moment 1 maps are displayed in the left middle and right middle panels respectively. The dotted white ellipse indicates the source region (6.5" radius). In the moment 0 map, the beam size is indicated by the solid white ellipse in the lower left corner and a 10 kpc scale bar is given in the top right. The far right panel shows the spectrum of the galaxy: the solid blue line is calculated with masking, the dotted green line is without.

B. MOMENT MAPS

In this appendix, we present the moment maps, optical images and spectra of the CO emission in the EGNoG bin C galaxies. Figure 7 shows the $CO(J = 1 \rightarrow 0)$ emission in galaxy C1 (we do not detect $CO(J = 3 \rightarrow 2)$ emission in galaxy C1). Figures 8 - 10 show both $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ emission in galaxies C2, C3 and C4, using all uv data and matched uv data.

C. RADIAL DEPENDENCE OF R_{31}

Since r_{31} traces the local excitation conditions of the molecular gas of a galaxy, it is expected to vary within the disk of the galaxy. In fact, Dumke et al. (2001) found $CO(J = 3 \rightarrow 2)$ emission to be more centrally concentrated than $CO(J = 1 \rightarrow 0)$ emission in nearby galaxies, so that r_{31} decreased with radius. To look for radial variation in r_{31} in the EGNoG data, we cannot compare the emission maps directly due to the marginal resolution of the galaxies and the different uv coverage of the two transitions. We emphasize that the uv coverage (and thus different spatial resolution) of each transition determines the shape of the radial profile of the enclosed flux (see Figure 6 in Appendix A), making a direct ratio of the two radial profiles meaningless without perfectly matched uv sampling (even our matched uv data do not meet this criterion due to different sampling within the allowed uv-distance range).

In order to disentangle the true emission distribution from the uv sampling, we fit a two-dimensional Gaussian to the total intensity (moment 0) map of each CO transition using the MIRIAD program imfit. The program fits for the position, peak intensity, total flux, size, and deconvolved source size. We perform the Gaussian fit on four versions of the moment 0 map for each transition in each galaxy: for each uv data selection (all and matched), we use moment 0 maps produced with and without 2σ smooth masking. In order to derive a good fit to the source emission, we restrict the Gaussian fit to the standard source region (Section A.2). The error in the fit total flux is calculated by proparting the errors on the fit peak intensity and (not deconvolved) size. Since these parameters are not independent, this error is likely an overestimate of the true error in the fit total flux.

The residual of each fit is inspected. We note that in general, the emission is fairly well fit by a Gaussian except for the $CO(J = 3 \rightarrow 2)$ transition in galaxies C2 and C3, which are observed at higher resolution. The structure present it in these higher resolution images is not well-fit by a Gaussian.

We look for a radial dependence in r_{31} by comparing the ratio calculated from the fit total fluxes to the ratio calculated from the deconvolved peak intensities. The results are presented in Table 6. For each galaxy, for each combination of uv data selection (all, matched) and masking (no mask, masked), we derive the deconvolved peak brightness temperature (T_b) for each CO transition and calculate r_{31} from the deconvolved peak intensities as well as the fit total fluxes (all values and errors are derived from the parameters of the Gaussian fitting) The rest-frame peak brightness temperature (in K) is given by

$$T_{\rm b} = \frac{h\nu_0}{k_{\rm B}\ln\left[\frac{2h\nu_0^3}{c^2(1+z)^3 I_{\rm peak}} + 1\right]} \tag{C1}$$

where ν_0 is the rest frequency of the transition and I_{peak} is the observed peak specific intensity (erg s⁻¹ cm⁻² Hz⁻¹ Sr⁻¹). We calculate I_{peak} from the velocity width (ΔV in km s⁻¹), fit total flux (S_{CO} in Jy km s⁻¹) and fit deconvolved size (FWHM_{major} and FWHM_{minor} in arcseconds):

$$I_{\rm peak} = \frac{4(\ln 2)(206265^2)S_{\rm CO}}{\pi(10^{23})\Delta V \rm FWHM_{\rm major} \rm FWHM_{\rm minor}}$$
(C2)

The ratio of the lines, r_{31} , is calculated from the line flux (total or peak) according to Equations 2 and 3. Note that this ratio is not equivalent to the ratio of the brightness temperatures as defined here (see discussion in Section 5).

The errors in the quantities given in Table 6 are calculated from the errors in the relevant fit parameters reported by imfit. We estimate the error in the deconvolved source sizes (FWHM_{major} and FWHM_{minor}) from the spread in the four estimates (all and matched uv, with and without masking) for each transition, for each galaxy. For each quantity,



Figure 8. Two sets of 6 panels showing the optical image (top left), moment maps (middle and right panels) and spectra (bottom left) for source C2: the top set uses all uv data, the bottom set uses matched uv data. In each set, the top middle and right panels show the moment 0 (total intensity) and moment 1 (intensity-weighted mean velocity) maps, respectively, for the $CO(J = 1 \rightarrow 0)$ line. The bottom middle and right panels show the same, but for the $CO(J = 3 \rightarrow 2)$ line. The synthesized beam (solid white ellipse) and 10 kpc scale (white bar) are indicated in each middle panel. The dotted white circles in the middle and right panels show the source regions in which flux is summed (with radii of 6.5" and 4.5" for the $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ data respectively; see Section A.2). The bottom left panels show the spectra in mJy, with the $CO(J = 3 \rightarrow 2)$ spectrum reduced by a factor of 4.5 to match the scale of the $CO(J = 1 \rightarrow 0)$ spectrum.



C3 : all uv

Figure 9. Same as Figure 8, but for source C3.



C4 : all uv

Figure 10. Same as Figure 8, but for source C4.

we report the average value for each galaxy, taking the error to be the average fractional error. From the average values, we report the mean (with an uncertainty from the errors in the average values) and standard deviation for the sample as a whole.

We find peak brightness temperatures of approximately 2 K and 4 K for $CO(J = 1 \rightarrow 0)$ and $CO(J = 3 \rightarrow 2)$ respectively. This is lower than the excitation temperature observed in Giant Molecular Clouds (GMCs) in the Milky Way (e.g. 10-30 K, Polychroni et al. 2012), as expected since the filling factor for GMCs in the molecular gas disk is less than unity.

While the value of r_{31} is a complex problem (discussed in detail in Section 5), the larger brightness temperature of the $CO(J = 3 \rightarrow 2)$ line (relative to the $CO(J = 1 \rightarrow 0)$ line) may be explained simply by differing excitation temperatures or filling factors. For instance, if the $CO(J = 1 \rightarrow 0)$ traces an additional diffuse, lower-excitation gas component not traced by the $CO(J = 3 \rightarrow 2)$ line (as observed in SMGs by Carilli et al. 2010; Riechers et al. 2011), the average brightness temperature of the $CO(J = 3 \rightarrow 2)$ line will be higher than the $CO(J = 1 \rightarrow 0)$ line. On the other hand, a larger brightness temperature in the $CO(J = 3 \rightarrow 2)$ line may be due to a larger filling factor for the $CO(J = 3 \rightarrow 2)$ emission. Our Gaussian fits find systematically smaller sizes for the $CO(J = 3 \rightarrow 2)$ emission relative to the $CO(J = 1 \rightarrow 0)$ sizes, which is consistent with the results of Dumke et al. (2001), who found $CO(J = 3 \rightarrow 2)$ emission to be more centrally concentrated than $CO(J = 1 \rightarrow 0)$ emission in nearby galaxies. Since the molecular gas disks of galaxies tend to have an exponential radial profile (e.g. Regan et al. 2001; Leroy et al. 2009), the gas-rich central region of the galaxy will account for a larger fraction of the $CO(J = 3 \rightarrow 2)$ emission area, increasing the effective filling factor of the $CO(J = 3 \rightarrow 2)$ emission relative to that of the $CO(J = 1 \rightarrow 0)$ emission. Assuming a constant excitation temperature for both transitions, the larger effective filling factor of $CO(J = 3 \rightarrow 2)$ emission would produce a higher brightness temperature, as we observe.

While the error bars are large, we do find the ratio of the deconvolved peak intensities (representative of the conditions in the central region of the galaxy) to be systematically higher than the ratio of the total fluxes. In our sample, we find $r_{31}(\text{peak}) = 0.73 \pm 0.31$, with a standard deviation across the three galaxies of 0.04. We compare this to the ratio calculated from total fluxes: 0.42 ± 0.11 , with a standard deviation of 0.04. While the small standard deviations in our r_{31} values show consistency between the three galaxies, these results are plagued by sizable uncertainties as a result of fitting data with only modest signal to noise (note that our error estimates are conservative and may in fact be over-estimating the true error). Therefore, we conclude (but not robustly) that r_{31} is higher in the center of the EGNoG galaxies than in the molecular disk as a whole (consistent with Dumke et al. 2001).

Na-	uv	Gaussian Fit Peak $T_{\rm b}$		Gaussia	Gaussian Fit r_{31}		
me	Sel.	CO(1-0)	CO(3-2)	Peak	Total		
C2	all	1.83 ± 0.32	3.79 ± 0.40	0.75 ± 0.54	0.41 ± 0.26		
		1.83 ± 0.32	3.71 ± 0.34	0.68 ± 0.47	0.48 ± 0.29		
	mat	1.91 ± 0.13	-	-	0.37 ± 0.13		
		1.90 ± 0.15	3.86 ± 0.47	0.72 ± 0.42	0.42 ± 0.20		
	avg	1.87 ± 0.23	3.79 ± 0.40	0.72 ± 0.48	0.42 ± 0.22		
C3	all	1.78 ± 0.32	3.45 ± 0.35	0.53 ± 0.40	0.44 ± 0.14		
		1.65 ± 0.27	3.51 ± 0.51	0.74 ± 0.67	0.38 ± 0.22		
	mat	1.68 ± 0.28	3.75 ± 0.37	0.94 ± 0.67	0.35 ± 0.07		
		1.65 ± 0.27	3.65 ± 0.38	0.88 ± 0.66	0.36 ± 0.11		
	avg	1.69 ± 0.28	3.59 ± 0.40	0.77 ± 0.60	0.38 ± 0.13		
C4	all	2.03 ± 0.60	4.10 ± 0.40	0.76 ± 0.72	0.48 ± 0.38		
		2.09 ± 0.33	4.16 ± 0.44	0.74 ± 0.46	0.45 ± 0.16		
	mat	2.08 ± 0.36	3.89 ± 0.31	0.57 ± 0.34	0.50 ± 0.15		
		2.23 ± 0.37	-	-	0.45 ± 0.19		
	avg	2.11 ± 0.42	4.05 ± 0.38	0.69 ± 0.50	0.47 ± 0.22		
mean		1.89 ± 0.19	3.81 ± 0.23	0.73 ± 0.31	0.42 ± 0.11		
σ		0.21	0.23	0.04	0.04		

Table 6

Gaussian fit T_b and r_{31} . Deconvolved, rest-frame peak brightness temperatures (peak T_b) and r_{31} calculated from the deconvolved peak intensities (r_{31} peak) and from the total fluxes (r_{31} total). All values are calculated using the parameters obtained from the Gaussian fitting. For each galaxy, we report five values in each column: one for each of the four data selections used (all uv (all) and matched uv(mat), with or without masking; presented in the same order as Table ??) and the average value with a typical error. From the average values for each galaxy, we calculate the mean (with an uncertainty from the errors in the average values) and the standard deviation for each quantity, presented in the bottom rows.