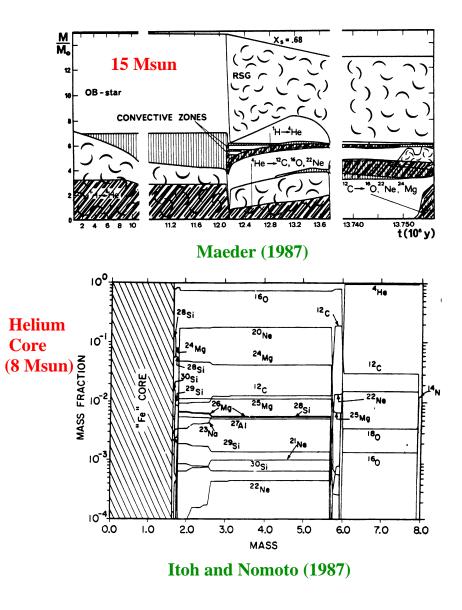
Evolution of Massive Stars



6.3 EVOLUTION OF MASSIVE STARS $(M \gtrsim 13 \, M_{\odot})$ (CO: 13.3)

- massive stars continue to burn nuclear fuel beyond hydrogen and helium burning and ultimately form an iron core
- alternation of nuclear burning and contraction phases

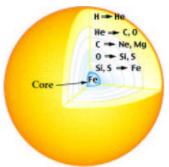
 \triangleright carbon burning $(T\sim 6\times 10^8\,K)$

$$\begin{array}{rcl} ^{12}\!C + ^{12}\!C & \rightarrow & ^{20}\!Ne + ^{4}\!He \\ & \rightarrow & ^{23}\!Na + ^{1}\!H \\ & \rightarrow & ^{23}\!Mg + n \end{array}$$

ho oxygen burning $(T \sim 10^9 \, {
m K})$

$$\begin{array}{rcl} {}^{16}\!O + {}^{16}\!O & \rightarrow & {}^{28}\!Si + {}^{4}He \\ & \rightarrow & {}^{31}\!P + {}^{1}H \\ & \rightarrow & {}^{31}\!S + n \\ & \rightarrow & {}^{30}\!S + 2 \, {}^{1}\!H \\ & \rightarrow & {}^{24}\!Mg + {}^{4}He + {}^{4}He \end{array}$$

 \triangleright silicon burning: photodisintegration of complex nuclei, hundreds of reactions \rightarrow iron



▷ form iron core

- ▷ iron is the most tightly bound nucleus \rightarrow no further energy from nuclear fusion
- iron core surrounded by onion-like shell structure

6.4.1 EXPLOSION MECHANISMS (ZG: 18-5B/C/D)

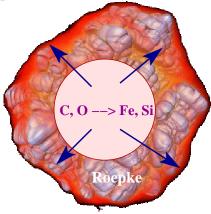
• two main, completely different mechanisms

Core-Collapse Supernovae



- triggered after the exhaustion of nuclear fuel in the core of a massive star, if the iron core mass > Chandrasekhar mass
- energy source is gravitational energy from the collapsing core ($\sim 10 \%$ of neutron star rest mass $\sim 3 \times 10^{46} \, J$)
- most of the energy comes out in neutrinos (SN 1987A!)
 - ▷ unsolved problem: how is some of the neutrino energy deposited ($\sim 1\%$, 10^{44} J) in the envelope to eject the envelope and produce the supernova?
- leaves compact remnant (neutron star/black hole)

Thermonuclear Explosions

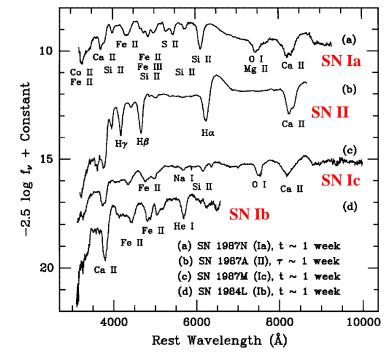


- occurs in accreting carbon/oxygen white dwarf when it reaches the Chandrasekhar mass
 - $\label{eq:carbon ignited under degenerate conditions;} \\ nuclear burning raises T, but not P$
 - \rightarrow thermonuclear runaway
 - $\rightarrow~$ incineration and complete destruction of the star
- energy source is nuclear energy (10^{44} J)
- no compact remnant expected
- main producer of iron
- standard candle (Hubble constant, acceleration of Universe?)

but: progenitor evolution not understood

- single-degenerate channel: accretion from nondegenerate companion
- b double-degenerate channel: merger of two CO white dwarfs

312 FILIPPENKO Supernova Classification



6.4.2 SUPERNOVA CLASSIFICATION

observational:

- Type I: no hydrogen lines in spectrum
- Type II: hydrogen lines in spectrum

theoretical:

- thermonuclear explosion of degenerate core
- $\bullet \ core \ collapse \rightarrow neutron \ star/black \ hole$

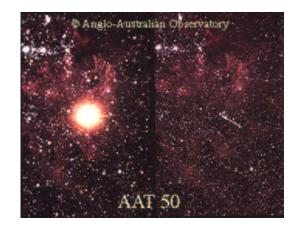
relation no longer 1 to $1 \rightarrow \text{confusion}$

- Type Ia (Si lines): thermonuclear explosion of white dwarf
- Type Ib/Ic (no Si; He or no He): core collapse of He star
- Type II-P: "classical" core collapse of a massive star with hydrogen envelope
- Type II-L: supernova with linear lightcurve (thermonuclear explosion of intermediate-mass star? probably not!)

complications

- special supernovae like SN 1987A
- Type IIb: supernovae that change type, SN 1993J (Type II \rightarrow Type Ib)
- some supernova "types" (e.g., IIn) occur for both explosion types ("phenomenon", not type; also see SNe Ic)
- new types: thermonuclear explosion of He star (Type Iab?)

SN 1987A (LMC)





IMB Implication <thImplication</th> <thImp

time in seconds

6.4.3 SN 1987A (ZG: 18-5)

- SN 1987A in the Large Magellanic Cloud (satellite galaxy of the Milky Way) was the first naked-eye supernova since Kepler's supernova in 1604
- long-awaited, but highly unusual, anomalous supernova
 - > progenitor blue supergiant instead of red supergiant
 - ▷ complex presupernova nebula
 - b chemical anomalies: envelope mixed with part of the helium core

Confirmation of core collapse

- neutrinos $(\bar{\nu}_e + p \rightarrow n + e^+)$, detected with Kamiokande and IMB detectors
 - ▷ confirmation: supernova triggered by core collapse
 - ▷ formation of compact object (neutron star)
 - \triangleright energy in neutrinos $(\sim 3\times 10^{46}\,J)$ consistent with the binding energy of a neutron star

Neutrino Signal

SUMMARY V: THE END STATES OF STARS

Three (main) possibilities

- the star develops a degenerate core and nuclear burning stops (+ envelope loss) → degenerate dwarf (white dwarf)
- the star develops a degenerate core and ignites nuclear fuel explosively (e.g. carbon) \rightarrow complete disruption in a supernova
- the star exhausts all of its nuclear fuel and the core exceeds the Chandrasekhar mass \rightarrow core collapse, compact remnant (neutron star, black hole)

Final fate as a function of initial mass (M_0) for Z = 0.02

$M_0 \lesssim 0.08M_\odot$	no hydrogen burning(degeneracy pressure+ Coulomb forces)	planets, brown dwarfs
$\left[0.08, 0.48 ight] \mathrm{M}_{\odot}$	hydrogen burning, no helium burning	degenerate He dwarf
$\left[0.48,8 ight] \mathbf{M}_{\odot}$	hydrogen, helium burning	degenerate CO dwarf
$[8,13]{ m M}_{\odot}$	complicated burning sequences, no iron core	neutron star
$\left[{{f 13},80} ight]{f M}_{\odot}$	formation of iron core, core collapse	neutron star, black hole
$M_0 \gtrsim 80M_\odot$	pair instability? complete disruption?	no remnant
also (?) $[6,8]\mathrm{M}_{\odot}$	degenerate carbon ignition possible (but unlikely), complete disruption	no remnant

SUMMARY III(B): IMPORTANT STELLAR TIMESCALES

• dynamical timescale: $t_{dyn} \simeq \frac{1}{\sqrt{4G\rho}}$ $\sim 30 \min \left(\rho / 1000 \, \text{kg} \, \text{m}^{-3} \right)^{-1/2}$

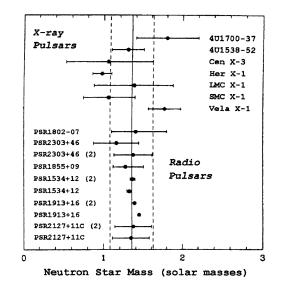
• thermal timescale (Kelvin-Helmholtz): $t_{KH} \simeq \frac{GM^2}{2RL}$ $\sim 1.5 \times 10^7 \, yr \, (M/M_{\odot})^2 \, (R/R_{\odot})^{-1} \, (L/L_{\odot})^{-1}$

• nuclear timescale: $t_{nuc} \simeq \underbrace{M_c/M}_{core\ mass} \underbrace{\eta}_{efficiency} (Mc^2)/L \\ \sim 10^{10} \, yr \, (M/M_{\odot})^{-3}$

Example	$\mathbf{t}_{\mathbf{dyn}}$	$t_{\rm KH}$	$\mathbf{t}_{\mathbf{nuc}}$
main-sequence stars			
$\begin{array}{l} {\rm a)} \ {\rm M} = 0.1 {\rm M}_{\odot}, \\ {\rm L} = 10^{-3} {\rm L}_{\odot}, \ {\rm R} = 0.15 {\rm R}_{\odot} \end{array}$	4 min	$10^9{ m yr}$	$10^{12}{ m yr}$
$f b) {f M} = 1 {f M}_{\odot}, {f L} = 1 {f L}_{\odot}, \ {f R} = 1 {f R}_{\odot}$	30 min	$15 imes 10^6{ m yr}$	$10^{10}{ m yr}$
$egin{array}{lll} { m c)} \ { m M} = 30 \ { m M}_{\odot}, \ { m L} = 2 imes 10^5 \ { m L}_{\odot}, \ { m R} = 20 \ { m R}_{\odot} \end{array}$	400 min	$3 imes 10^3{ m yr}$	$2 imes 10^6{ m yr}$
$egin{array}{lll} {f red \ giant} & ({ m M}=1{ m M}_{\odot}, \ { m L}=10^3~{ m L}_{\odot}, \ { m R}=200{ m R}_{\odot}) \end{array}$	$50\mathrm{d}$	$75{ m yr}$	
$egin{array}{lll} {f white \ dwarf} \ ({ m M} = 1 { m M}_{\odot}, \ { m L} = 5 imes 10^{-3} { m L}_{\odot}, \ { m R} = 2.6 imes 10^{-3} { m R}_{\odot}) \end{array}$	$7\mathrm{s}$	$10^{11}{ m yr}$	
$\begin{array}{l} {\rm neutron \ star} \ ({\rm M} = 1.4 {\rm M}_{\odot}, \\ {\rm L} = 0.2 \ {\rm L}_{\odot}, \ {\rm R} = 10 {\rm km}, \\ {\rm T}_{\rm eff} = 10^6 {\rm K}) \end{array}$	$0.1\mathrm{ms}$	$10^{13}{ m yr}$	

6.4.4 NEUTRON STARS (ZG: 17-2; CO: 15.6)

- are the end products of the collapse of the cores (mainly Fe) of massive stars (between 8 and $\sim 20 \, M_{\odot}$)
- in the collapse, all nuclei are dissociated to produce a very compact remnant mainly composed of neutrons and some protons/electrons
 - Note: this dissociation is endothermic, using some of the gravitational energy released in the collapse
 - b these reactions undo all the previous nuclear fusion reactions
- since neutrons are fermions, there is a maximum mass for a neutron star (similar to the Chandrasekhar mass for white dwarfs), estimated to be between $1.5-3 M_{\odot}$
- typical radii: 10 km (i.e. density $\sim 10^{18} \, \mathrm{kg} \, \mathrm{m}^{-3}!)$



6.4.5 SCHWARZSCHILD BLACK HOLES (ZG: 17-3; CO: 16)

- event horizon: (after Michell 1784)
 - ▷ the escape velocity for a particle of mass m from an object of mass M and radius R is $v_{esc} = \sqrt{\frac{2GM}{R}}$ (11 km s⁻¹ for Earth, 600 km s⁻¹ for Sun)
 - \triangleright assume photons have mass: $m \propto E$ (Newton's corpuscular theory of light)
 - ▷ photons travel with the speed of light c
 - $\rightarrow~$ photons cannot escape, if $v_{esc} > c$

$$\rightarrow \boxed{R < R_s \equiv \frac{2GM}{c^2}} \text{ (Schwarzschild radius)}$$

 $hinspace{-1.5}{
m P} {
m R}_{
m s} = 3\,{
m km}\,({
m M}/\,{
m M}_{\odot})$

Note: for neutron stars $R_s\simeq 5\,km;$ only a factor of 2 smaller than $R_{NS}\to GR$ important

Orbits near Schwarzschild Black Holes

