High Energy Astrophysics Dr. Adam Ingram



Schedule

- Lecture 1: Shocks Blast waves from huge explosions, strong shock conditions at the front of the blast wave.
- Lecture 2: Shock Acceleration How electrons are accelerated to ultra-relativistic energies at strong shock fronts.
- Lecture 3: Synchrotron Radiation The emission mechanism.
- Lecture 4: Synchrotron Radiation Synchrotron self-absorption and spectral ageing.
- Lecture 5: Accretion discs Structure, luminosity and spectrum.
- Lecture 6: The X-ray Corona Thermal Compton scattering, X-ray reflection.
- Lecture 7: Black holes and Jets The AGN zoo, evidence for black holes, jet mechanisms, super-luminal jet motion.
- Lecture 8: Galaxy Clusters Thermal bremsstrahlung radiation, Sunyaev-Zeldovich effect.

Reading Material

- "High Energy Astrophysics" by Malcolm Longair
- "Accretion Power in Astrophysics" by Frank, King & Raine
- "Radiative Processes in Astrophysics" by Rybicki & Lightman

Questions: Online question session, can also email me!

Lecture 1 Shocks





0.025 SEC.

100 METERS

After an explosion (e.g. supernova, atomic bomb) a fireball expands outwards



- In 1950, G. I. Taylor calculated how the fireball expansion relates to explosion energy and external density
- He reduced the problem to a self-similar scaling solution basically using dimensional analysis.
- He reasoned that r is a function of E, ρ and t:

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- He reasoned that r is a function of E, ρ and t:



 $r = C\rho^x E^y t^z$

 $r = C\rho^{x}E^{y}t^{z}$ $\implies m = [\text{kg m}^{-3}]^{x} [\text{kg m}^{2} \text{ s}^{-2}]^{y} [s]^{z}$ $m = \text{kg}^{x+y} \text{ m}^{-3x+2y} \text{ s}^{-2y+z}$

 $r = C\rho^{x}E^{y}t^{z}$ $m = [kg m^{-3}]^{x} [kg m^{2} s^{-2}]^{y} [s]^{z}$ $m = kg^{x+y} m^{-3x+2y} s^{-2y+z}$ 0 = x + y...mass 1 = -3x + 2y...length 0 = -2y + z...time

Blast waves $r = C\rho^x E^y t^z$ 0 = x + y1 = -3x + 2y0 = -2y + zx = -1/5y = 1/5z = 2/5

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 $r = C\rho^{-1/5}E^{1/5}t^{2/5}$ $\implies r^5\rho$ $E = D\frac{r^5\rho}{t^2}$

- Taylor used high-speed photographs of small detonations in the lab to determine that D~1.033 for a fireball expanding into air.
- The power of dimensional analysis is that even though the experiments were done on very small scales, we can be sure the scaling will still hold for explosions that are many, many orders of magnitude greater.
- Sedov later came up with a full solution (see: http://www.mso.anu.edu.au/~geoff/AGD/Sedov.pdf), and so the above formula is usually referred to as the *Taylor-Sedov solution*.

• Taylor used his equation and de-classified photos of the 1st atomic bomb tests to calculate the yield of the bomb.

 $E \approx 1.033 \frac{r^{5} \rho}{t^{2}}$ $\rho \approx 1.1 \text{ kg m}^{-3}$ $r \approx 140 \text{ m}$ t = 25 ms $E \approx 9.778 \times 10^{13} \text{ J}$ $E \approx 23.28$ kilotons



 $E \approx 23.28$ kilotons

- Taylor used his equation and de-classified photos of the 1st atomic bomb tests to calculate the yield of the bomb.
- The true (still classified in 1950) yield of the bomb was ~18-20 kilotons!!



- Now calculate fluency of the Crab supernova of 1054 $E \approx \frac{r^5 \rho}{t^2}$
- $\rho \approx 10^{-21} \text{ kg m}^{-3}$ $r \approx 3 \text{ pc} \sim 9 \times 10^{16} \text{ m}$ $t = 966 \text{ yrs} \sim 3 \times 10^{10}$

 $E \approx 6.6 \times 10^{42} \text{ J}$



• What about the current speed of the blast wave?

 $\dot{r} \approx 1.2 \times 10^6$ m/s

 $\dot{r} \approx (2/5)\rho^{-1/5}E^{1/5}t^{-3/5}$



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Blast wave is supersonic!



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Shock!



- A shock occurs when a disturbance moves through a medium faster than the sound speed in the medium, i.e., sufficiently fast that a pressure wave cannot precede the disturbance.
- The conditions in the medium—temperature, density, bulk velocity —thus change almost instantaneously at the shock. The material which is hit by the shock receives no forewarning.



Derivation of strong shock 'jump conditions'



Switch to rest frame of the shock





(1) Mass conservation:

$$\rho_d v_d = \rho_u v_u$$

Mass per unit area flowing across shock front



(2) Momentum conservation:

Momentum per unit area flowing across shock front

$$P_d + \rho_d v_d^2 = P_u + \rho_u v_u^2$$



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Ram pressure (pressure from bulk motion)



(2) Momentum conservation:

Momentum per unit area flowing across shock front





Ram pressure (pressure from bulk motion)



(3) Energy conservation:

Energy per unit area flowing across shock front



(3) Energy conservation:

Energy per unit area flowing across shock front

$$v_d \left[\frac{1}{2}\rho_d v_d^2 + \rho_d \epsilon_d\right] + P_d v_d = v_u \left[\frac{1}{2}\rho_u v_u^2 + \rho_u \epsilon_u\right] + P_u v_u$$

 ϵ = internal energy per unit mass



(3) Energy conservation:

Energy per unit area flowing across shock front



 ϵ = internal energy per unit mass



Rankine-Hugoniot jump conditions:

1)
$$\rho_d v_d = \rho_d v_u$$

2) $P_d + \rho_d v_d^2 = P_u + \rho_u v_u^2$
3) $v_d \left[\frac{1}{2} \rho_d v_d^2 + \rho_d \epsilon_d \right] + P_d v_d = v_u \left[\frac{1}{2} \rho_u v_u^2 + \rho_u \epsilon_u \right] + P_u v_u$



Simplify (2):

$$P_d + \rho_d v_d^2 = P_u + \rho_u v_u^2$$
$$T_u \sim 0 \implies P_u \sim 0 \implies$$
$$P_d + \rho_d v_d^2 = \rho_u v_u^2$$

$$\rho_d v_d = \rho_u v_u \tag{1}$$

$$P_d + \rho_d v_d^2 = \rho_u v_u^2 \tag{2}$$

$$(3)$$

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$$\tag{3}$$

Simplify (3):

$$v_d \left[\frac{1}{2} \rho_d v_d^2 + \rho_d \epsilon_d \right] + P_d v_d = v_u \left[\frac{1}{2} \rho_u v_u^2 + \rho_u \epsilon_u \right] + P_u v_u$$

$$\rho_d v_d = \rho_u v_u \tag{1}$$

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Simplify (3):

$$v_d \left[\frac{1}{2} \rho_d v_d^2 + \rho_d \epsilon_d \right] + P_d v_d = v_u \left[\frac{1}{2} \rho_u v_u^2 + \rho_u \epsilon_u \right] + P_u v_u$$

For ideal gas:

$$\epsilon = \frac{3}{2} \frac{kT}{\bar{m}}$$
 $P = \frac{\rho}{\bar{m}} kT$ \therefore $\rho \epsilon = \frac{3}{2}P$

$$\rho_d v_d = \rho_u v_u \tag{1}$$

$$P_d + \rho_d v_d^2 = \rho_u v_u^2 \tag{2}$$

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Simplify (3):

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For ideal gas:

$$\rho_{d}v_{d} = \rho_{u}v_{u}$$
(1)

$$\bigstar \qquad P_{d} + \rho_{d}v_{d}^{2} = \rho_{u}v_{u}^{2}$$
(2)

$$v_{d} \left[\frac{1}{2}\rho_{d}v_{d}^{2} + \frac{3}{2}P_{d}\right] + P_{d}v_{d} = v_{u}\frac{1}{2}\rho_{u}v_{u}^{2}$$
(3)

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$$\begin{aligned}
\rho_{d}v_{d} &= \rho_{u}v_{u} \quad (1) \\
\bigstar \quad P_{d} + \rho_{d}v_{d}^{2} &= \rho_{u}v_{u}^{2} \quad (2) \\
\frac{1}{2}\rho_{d}v_{d}^{3} + \frac{5}{2}P_{d}v_{d} &= \frac{1}{2}\rho_{u}v_{u}^{3} \quad (3)
\end{aligned}$$

(2)
$$\implies P_d = \rho_u v_u^2 - \rho_d v_d^2$$

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$$-\frac{1}{2}\rho_u v_u^3 - 2\rho_d v_d^3 + \frac{5}{2}\rho_u v_u^2 v_d = 0$$
$$\times -2$$

$$\rho_{u}v_{u}^{3} + 4\rho_{d}v_{d}^{3} - 5\rho_{u}v_{u}^{2}v_{d} = 0$$

Sub in (1):



$$\rho_{u}v_{u}^{3} + 4\frac{\rho_{u}^{3}}{\rho_{d}^{2}}v_{u}^{3} - 5\frac{\rho_{u}^{2}}{\rho_{d}}v_{u}^{3} = 0$$

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$$\rho_{u} \gamma_{u}^{3} + 4 \frac{\rho_{u}^{3}}{\rho_{d}^{2}} \gamma_{u}^{3} - 5 \frac{\rho_{u}^{2}}{\rho_{d}} \gamma_{u}^{3} = 0$$

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(3)

Strong shock jump conditions:



V_U

Back in the rest frame of the ISM

Assumptions:

- Ideal gas, T.E./m=(3/2)kT
- Mach number: $\mathcal{M} \equiv v/c_s \gg 1$
- T_u~0
- Ignored viscosity (only important within mean free path from shock front)



X-rays

Compact object: black hole / neutron star / white dwarf

Companion star

- Compact object = black hole or neutron star: system called an X-ray binary
- Compact object = white dwarf: system called cataclysmic variable or dwarf nova (historic)
- White dwarf systems: WD always observed to be more massive than companion
- High mass X-ray binaries (HMXBs):

$$\begin{split} M_{\rm companion} > M_{\rm co} \\ {\rm Low \ mass \ X-ray \ binaries \ (LMXBs):} \\ M_{\rm companion} < M_{\rm co} \end{split}$$

Compact object accretion LMXBs: Roche-Lobe Overflow

- Roche potential: companion star (CS) occupies equipotential surface.
- CS can fill its Roche Lobe if it swells during its evolution, or binary separation reduces due to angular momentum loss due to e.g. stellar wind mass loss or gravitational waves.
- Then material passes through L₁ (inner Lagrange point).
- In-falling material forms an accretion disc



HMXBs: Stellar Wind Capture

- $M \gtrsim 15 \ M_{\odot}$ stars can have a strong stellar wind.
- Wind can be captured by the compact object.
- Accretion luminosity therefore depends on mass outflow rate of wind.
- Can also get Roche-Lobe overflow in HMXBs, but less common
- Intermediate case: Cygnus X-1 has a focused wind



Magnetic fields

 B-field of NS / WD can interrupt disc and channel material directly to magnetic poles.



CV (white dwarf) / X-ray pulsar (neutron star)

Magnetic fields

- B-field of NS / WD can interrupt disc and channel material directly to magnetic poles.
- For strongest field WDs, there can be no disc at all.



Polar

Magnetic fields

- Gravitational free fall in accretion column
- Shock as material is halted
- Homework problem: calculate T_d (hot enough to emit hard Xrays)

ial is ial is ial is v_u = v_f $\downarrow \downarrow \downarrow \downarrow f$ hard X-X-ray $v_d \sim v_{ff}$

Magnetic pole

Shock

X-ray

 T_u

Neutron star / White dwarf