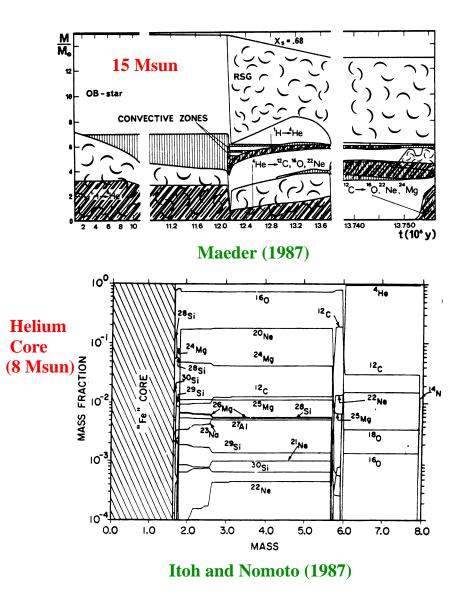
Evolution of Massive Stars



6.3 EVOLUTION OF MASSIVE STARS ($M \gtrsim 13 M_{\odot}$) (CO: 13.3)

- massive stars continue to burn nuclear fuel beyond hydrogen and helium burning and ultimately form an *iron core*
- \bullet alternation of nuclear $burning\ and\ contraction\ phases$

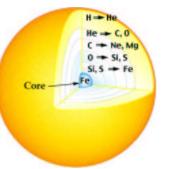
 $hightarrow carbon \ burning \ (T \sim 6 imes 10^8 \, {
m K})$

$$\begin{array}{rcl} ^{12}\!C + ^{12}\!C & \rightarrow & ^{20}\!Ne + ^{4}\!He \\ & \rightarrow & ^{23}\!Na + ^{1}\!H \\ & \rightarrow & ^{23}\!Mg + n \end{array}$$

 $ho \ oxygen \ burning \ ({
m T} \sim 10^9 \, {
m K})$

$$\begin{array}{rcl} {}^{16}\!O+^{16}O & \rightarrow & {}^{28}\!Si+{}^{4}He \\ & \rightarrow & {}^{31}\!P+{}^{1}H \\ & \rightarrow & {}^{31}\!S+n \\ & \rightarrow & {}^{30}\!S+2\,{}^{1}\!H \\ & \rightarrow & {}^{24}\!Mg+{}^{4}He+{}^{4}He \end{array}$$

 \triangleright silicon burning: photodisintegration of complex nuclei, hundreds of reactions \rightarrow iron



 \triangleright form *iron core*

- \triangleright *iron* is the most tightly *bound nucleus* \rightarrow no further energy from nuclear fusion
- > iron core surrounded by onion-like shell structure

6.4.1 EXPLOSION MECHANISMS (ZG: 18-5B/C/D)

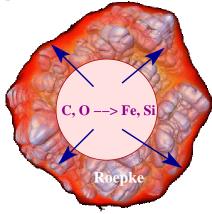
• two main, completely different mechanisms

Core-Collapse Supernovae



- triggered after the exhaustion of nuclear fuel in the core of a massive star, if the *iron core mass > Chandrasekhar mass*
- energy source is gravitational energy from the collapsing core ($\sim 10 \%$ of neutron star rest mass $\sim 3 \times 10^{46} \, J$)
- most of the energy comes out in *neutrinos* (SN 1987A!)
 - \triangleright unsolved problem: how is some of the neutrino energy deposited (~ 1%, 10⁴⁴ J) in the envelope to eject the envelope and produce the supernova?
- leaves compact remnant (neutron star/black hole)

Thermonuclear Explosions



- occurs in *accreting* carbon/oxygen *white dwarf* when it reaches the *Chandrasekhar mass*
 - \rightarrow carbon ignited under degenerate conditions; nuclear burning raises T, but not P
 - ightarrow thermonuclear runaway
 - $\rightarrow~$ incineration and complete~destruction of the star
- energy source is nuclear energy (10^{44} J)
- no compact remnant expected
- main producer of *iron*
- *standard candle* (Hubble constant, acceleration of Universe?)

but: progenitor evolution not understood

- \triangleright single-degenerate channel: accretion from nondegenerate companion
- ▷ *double-degenerate channel:* merger of two CO white dwarfs

6.4.2 SUPERNOVA CLASSIFICATION

observational:

- Type I: no hydrogen lines in spectrum
- Type II: hydrogen lines in spectrum

theoretical:

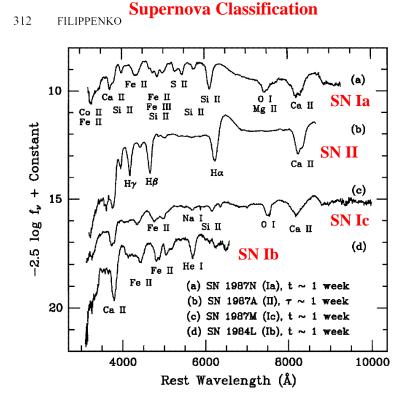
- thermonuclear explosion of degenerate core
- core collapse \rightarrow neutron star/black hole

relation no longer 1 to $1 \rightarrow confusion$

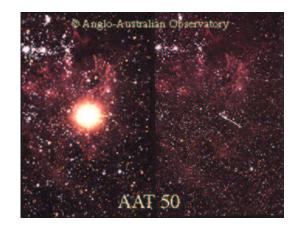
- *Type Ia* (Si lines): thermonuclear explosion of white dwarf
- *Type Ib/Ic* (no Si; He or no He): core collapse of He star
- *Type II-P:* "classical" core collapse of a massive star with hydrogen envelope
- *Type II-L:* supernova with linear lightcurve (thermonuclear explosion of intermediate-mass star? probably not!)

complications

- special supernovae like SN 1987A
- Type IIb: supernovae that change type, SN 1993J (Type II \rightarrow Type Ib)
- some supernova *"types"* (e.g., IIn) occur for both explosion types (*"phenomenon"*, not type; also see SNe Ic)
- new types: thermonuclear explosion of He star (Type Iab?)



SN 1987A (LMC)





IMB Implication <thImplication</th> <thImp

time in seconds

6.4.3 SN 1987A (ZG: 18-5)

- SN 1987A in the Large Magellanic Cloud (satellite galaxy of the Milky Way) was the first naked-eye supernova since Kepler's supernova in 1604
- long-awaited, but highly unusual, anomalous supernova
 - > progenitor blue supergiant instead of red supergiant
 - > complex presupernova nebula
 - ▷ *chemical anomalies:* envelope mixed with part of the helium core

Confirmation of core collapse

- neutrinos $(\overline{\nu}_e + p \rightarrow n + e^+)$, detected with Kamiokande and IMB detectors
 - ▷ confirmation: supernova triggered by core collapse
 - ▷ formation of compact object (neutron star)
 - ightarrow energy in neutrinos ($\sim 3 imes 10^{46} \, {
 m J}$) consistent with the binding energy of a neutron star

Neutrino Signal

SUMMARY III(B): IMPORTANT STELLAR TIMESCALES

• dynamical timescale: $t_{dyn} \simeq rac{1}{\sqrt{4G
ho}} \ \sim 30 \min \left(
ho / 1000 \, \mathrm{kg \, m^{-3}}
ight)^{-1/2}$

- thermal timescale (Kelvin-Helmholtz): $t_{KH} \simeq \frac{GM^2}{2RL}$ $\sim 1.5 \times 10^7 \, yr \, (M/M_{\odot})^2 \, (R/R_{\odot})^{-1} \, (L/L_{\odot})^{-1}$
- nuclear timescale: ${
 m t}_{
 m nuc} \simeq \underbrace{{
 m M}_c/{
 m M}}_{
 m core\ mass} \underbrace{\eta}_{
 m efficiency} ({
 m Mc}^2)/L \ \sim 10^{10}\,{
 m yr}\,\left({
 m M}/\,{
 m M}_\odot
 ight)^{-3}$

Example	${ m t_{dyn}}$	$t_{\rm KH}$	${ m t}_{ m nuc}$
main-sequence stars			
$egin{array}{lll} {f M} = 0.1{f M}_{\odot}, \ {f L} = 10^{-3}{f L}_{\odot}, \ {f R} = 0.15{f R}_{\odot} \end{array}$	$4 \min$	$10^9{ m yr}$	$10^{12}{ m yr}$
$egin{array}{lll} {f b} & {f M} = 1 {f M}_{\odot}, \ {f L} = 1 {f L}_{\odot}, \ {f R} = 1 {f R}_{\odot} \end{array}$	$30{ m min}$	$15 imes 10^6{ m yr}$	$10^{10}{ m yr}$
$egin{array}{lll} { m c} & { m M} = 30 \ { m M}_{\odot}, \ { m L} = 2 imes 10^5 \ { m L}_{\odot}, \ { m R} = 20 \ { m R}_{\odot} \end{array}$	400 min	$3 imes 10^3{ m yr}$	$2 imes 10^6{ m yr}$
$egin{array}{ll} red \; giant \; ({ m M}=1 { m M}_{\odot}, \ { m L}=10^3 \; { m L}_{\odot}, \; { m R}=200 { m R}_{\odot}) \end{array}$	$50\mathrm{d}$	$75{ m yr}$	
$egin{array}{lll} {\it white \ dwarf \ (M=1M_{\odot},\ L=5 imes 10^{-3}\ L_{\odot},\ R=2.6 imes 10^{-3}\ R_{\odot}) \end{array}$	$7\mathrm{s}$	$10^{11}{ m yr}$	
$egin{aligned} neutron\ star\ ({ m M} = 1.4\ { m M}_{\odot}, \ { m L} = 0.2\ { m L}_{\odot}, \ { m R} = 10\ { m km}, \ { m T}_{ m eff} = 10^6\ { m K}) \end{aligned}$	$0.1\mathrm{ms}$	$10^{13}{ m yr}$	

SUMMARY V: THE END STATES OF STARS

Three (main) possibilities

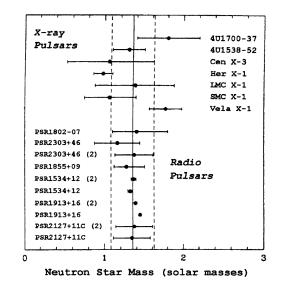
- the star develops a *degenerate core* and nuclear burning stops (+ envelope loss) \rightarrow *degenerate dwarf (white dwarf)*
- the star develops a degenerate core and ignites nuclear fuel explosively (e.g. carbon) \rightarrow complete disruption in a supernova
- the star *exhausts* all of its *nuclear fuel* and the core exceeds the *Chandrasekhar mass* \rightarrow *core collapse, compact remnant (neutron star, black hole)*

Final fate as a function of initial mass (M_0) for Z = 0.02

$M_0 \lesssim 0.08M_\odot$	no hydrogen burning (degeneracy pressure + Coulomb forces)	planets, brown dwarfs
$\left[0.08, 0.48 ight] \mathrm{M}_{\odot}$	hydrogen burning, no helium burning	$degenerate \; He \\ dwarf$
$[0.48,8]M_\odot$	<i>hydrogen, helium</i> burning	degenerate CO dwarf
$[8,13]\mathrm{M}_{\odot}$	<i>complicated</i> burning sequences, <i>no iron</i> core	neutron star
$[13,80]\mathbf{M}_{\odot}$	formation of <i>iron</i> core, <i>core collapse</i>	neutron star, black hole
$M_0 \gtrsim 80M_\odot$	pair instability? complete disruption?	no remnant
also (?) $[6,8]\mathrm{M}_{\odot}$	degenerate carbon ignition possible (but unlikely), complete disruption	no remnant

6.4.4 NEUTRON STARS (ZG: 17-2; CO: 15.6)

- are the end products of the *collapse* of the cores (mainly Fe) of massive stars (between 8 and $\sim 20 \, M_{\odot}$)
- in the collapse, all nuclei are dissociated to produce a very compact remnant mainly composed of *neutrons* and some *protons/electrons*
 - Note: this dissociation is *endothermic*, using some of the gravitational energy released in the collapse
 - \triangleright these reactions undo all the previous nuclear fusion reactions
- since neutrons are *fermions*, there is a *maximum* mass for a neutron star (similar to the Chandrasekhar mass for white dwarfs), estimated to be between $1.5 3 \,\mathrm{M}_{\odot}$
- typical radii: $10 \, km$ (i.e. density $\sim 10^{18} \, \mathrm{kg \, m^{-3}!})$



6.4.5 SCHWARZSCHILD BLACK HOLES (ZG: 17-3; CO: 16)

- event horizon: (after Michell 1784)
 - $\label{eq:constraint} \begin{array}{l} \triangleright \mbox{ the $escape$ velocity for a particle of mass m from} \\ \mbox{ an object of mass M and radius R is $v_{esc} = \sqrt{\frac{2GM}{R}} \\ \mbox{ (11 km s^{-1} for Earth, 600 km s^{-1} for Sun)} \end{array}$
 - \triangleright assume *photons* have *mass:* $m \propto E$ (Newton's corpuscular theory of light)
 - \triangleright photons travel with the speed of light c
 - $\rightarrow~$ photons cannot escape, if $v_{esc} > c$

$$ightarrow {f R} < {f R}_{s} \equiv {2GM \over c^2} \ (Schwarzschild \ radius)$$

 $hinspace{-1.5}{
m P} {
m R}_{
m s} = 3\,{
m km}\,({
m M}/\,{
m M}_{\odot})$

Note: for neutron stars $R_s\simeq 5\,km;$ only a factor of 2 smaller than $R_{NS}\rightarrow GR$ important

Orbits near Schwarzschild Black Holes

